

***Zawansowane Modelowanie  
i Analiza Systemów  
Informatycznych  
(1- 4)***



**Polsko-Japońska Wyższa Szkoła Technik Komputerowych  
Katedra Systemów Informacyjnych  
2012**

## *Overwiev*

- **The CSDP steps 4-6 ,**

**NOTE !!!!**

**This lecture covers LOTS of material – students' study will be necessary!!!!**

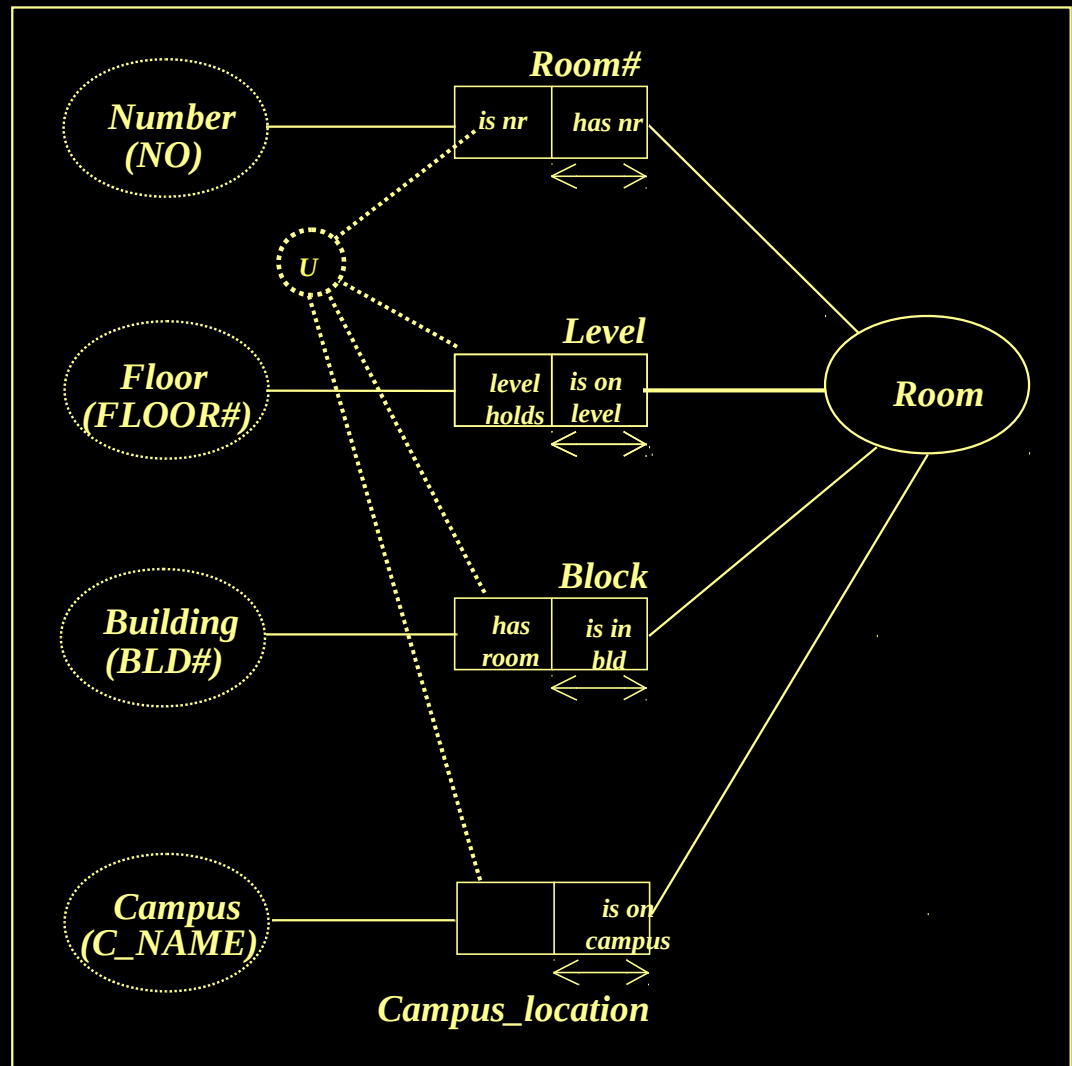
## *The 7 steps of CSDP*

- Step 1: transform familiar information examples into elementary facts, and apply quality checks**
- Step 2: draw the fact types, and apply a population check**
- Step 3: check for entity types that should be combined, and note any arithmetic derivations**
- Step 4: add uniqueness constraints, arity of fact types, splitting of fact types.**
- Step 5: add mandatory role constraints, and check for logical derivations**
- Step 6: add value, set comparison and subtyping constraints**
- Step 7: add other constraints and perform final quality checks (e.g., populating fact type instances)**

# Step 4 -Uniqueness constraints across several fact types

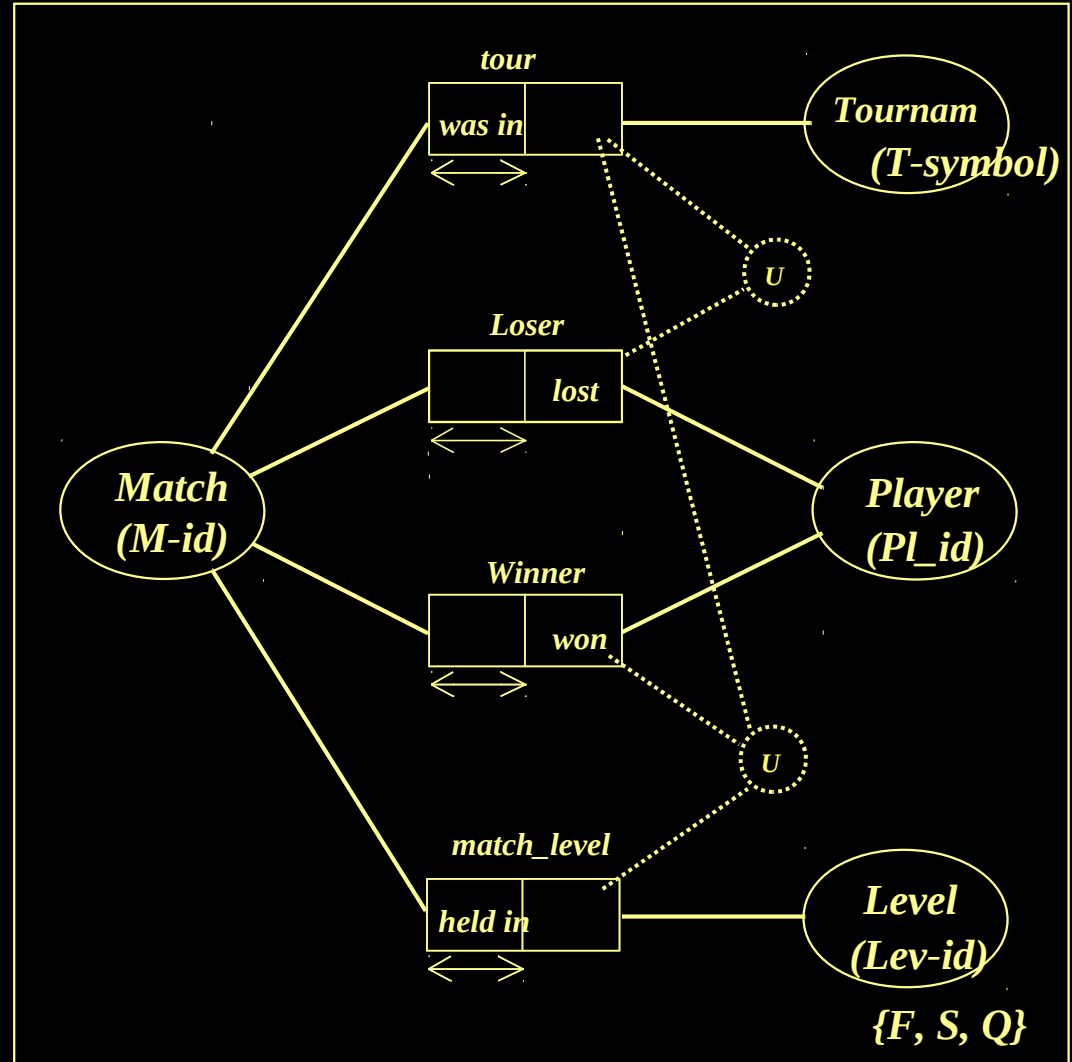
*A room is identified by  
Campus,  
Building,  
Level,  
Room number*

*Example:  
(Gardens, A, 3, 11)*

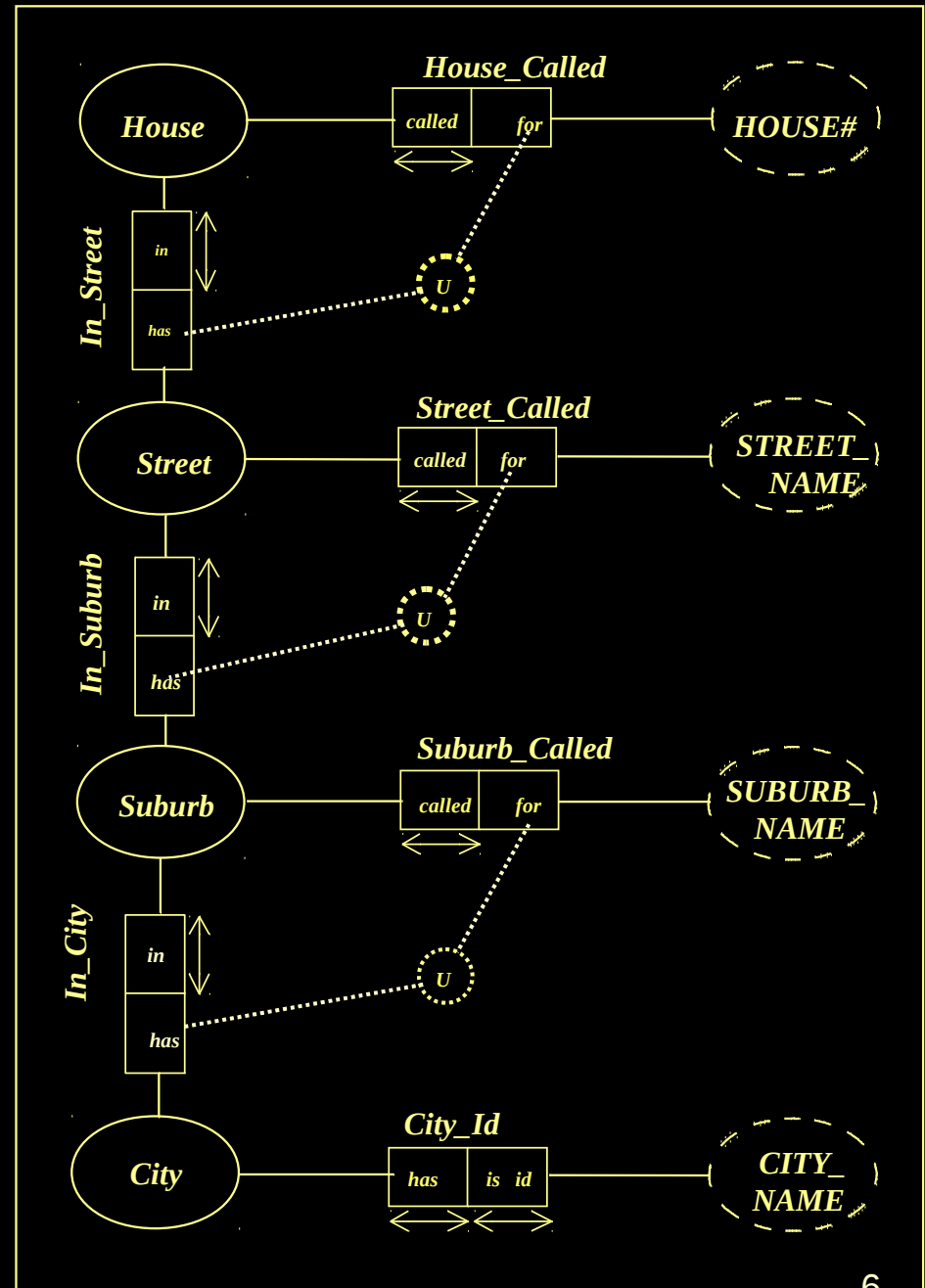


# Uniqueness constraints across several fact types 'Tennis Tournaments'

M-id	Tour	Lev	Win	Los
001	Wi	Q	A	H
002	Wi	Q	B	G
003	Wi	Q	C	F
004	Wi	Q	D	E
005	Wi	S	A	D
006	Wi	S	B	C
007	Wi	F	A	B
008	AO	Q	B	D
009	AO	S	D	J
.....				



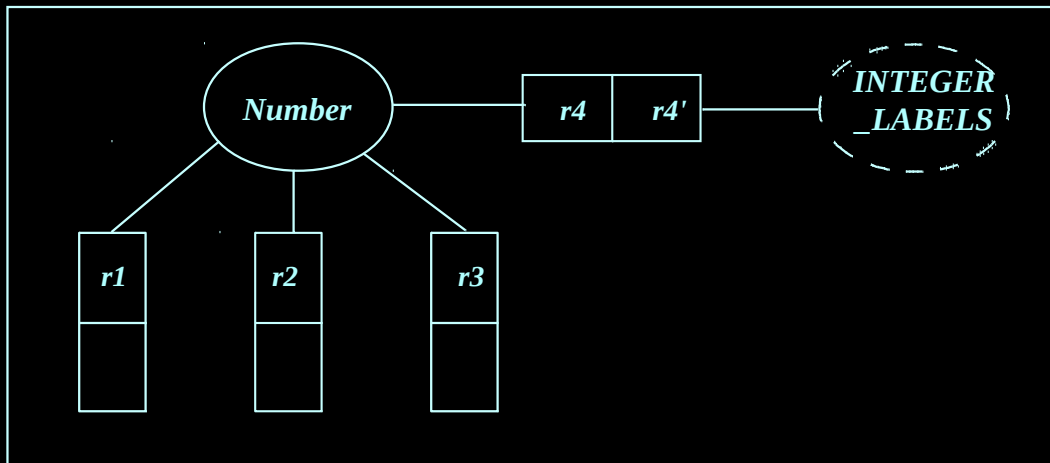
# Hierarchical Structures for entity type identification



# The distinction between entity types and label types:

The distinguishing characteristic of a label type is that it is involved in ONLY ONE ROLE

Illustration:

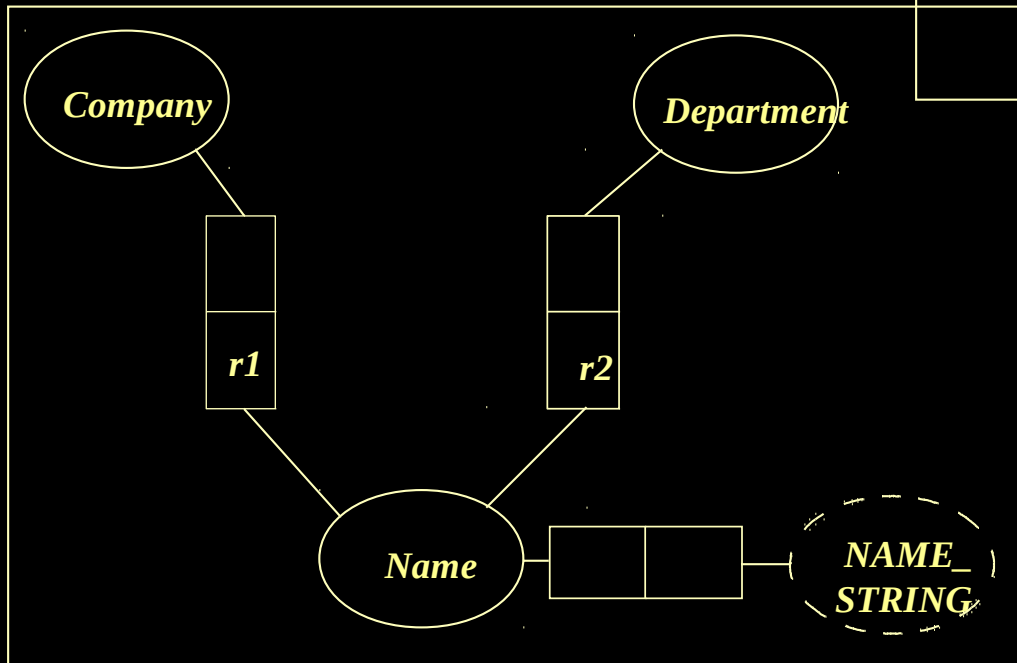
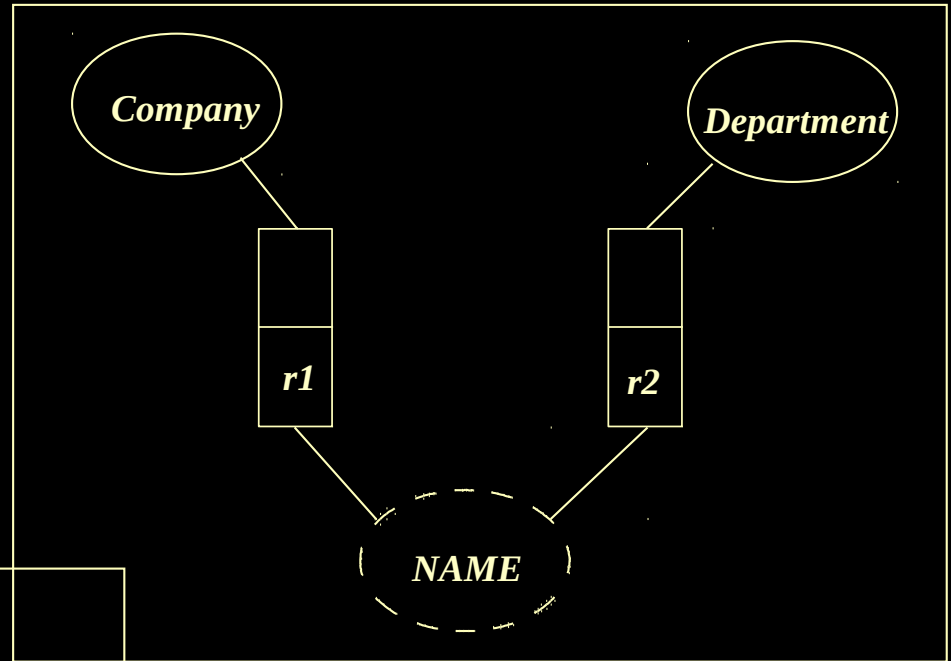


**Number** may be involved in many roles (r1, r2, r3, r4) and so is an entity type, whereas **INTEGER** is and will only ever be involved in one role r4'.

The following diagram is syntactically incorrect



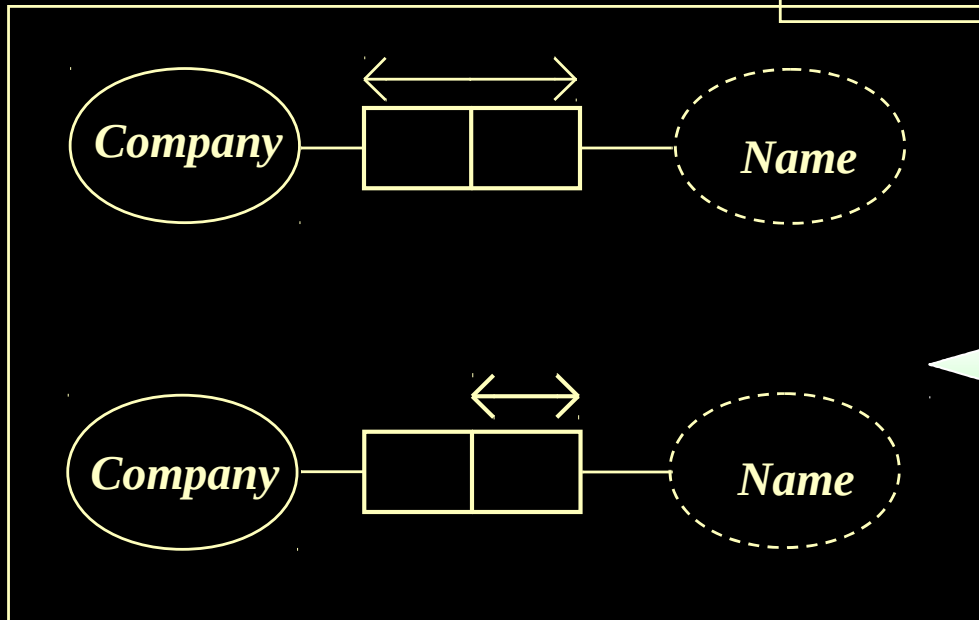
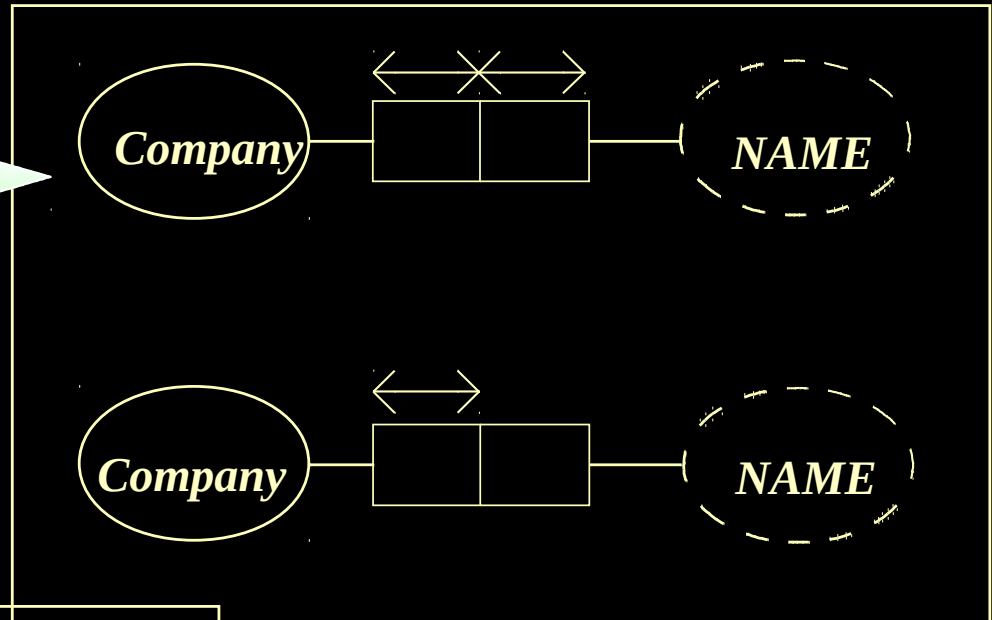
NAME is involved in two roles.  
Would the following declarations  
shown below be correct?





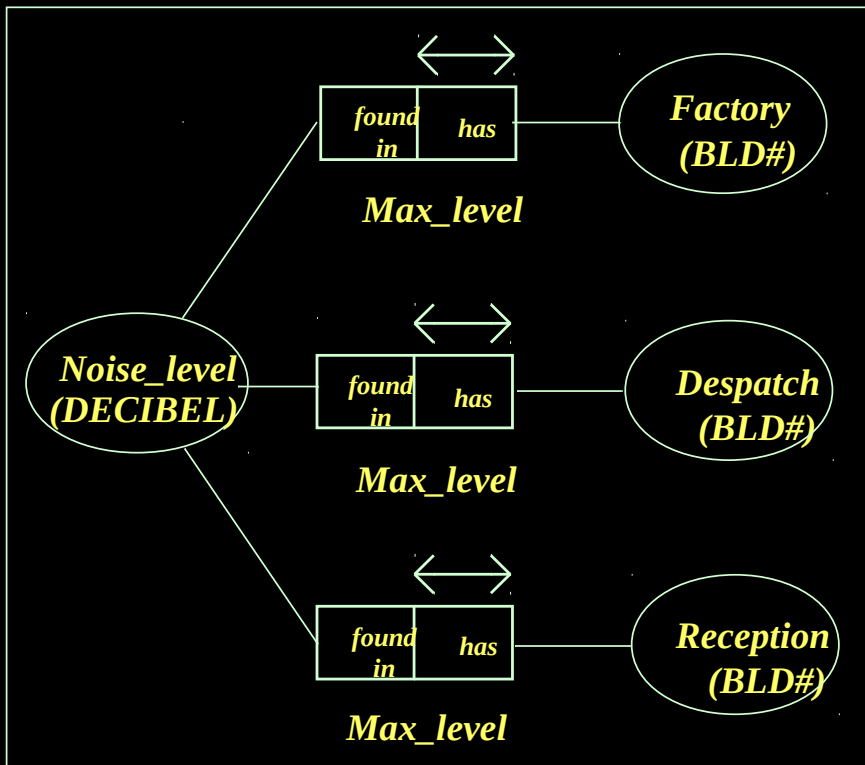
# Valid situations for UCons in declaration of label types

In the following situations NAME has to be an entity type, not a label type:



Incorrect schema

## Example:

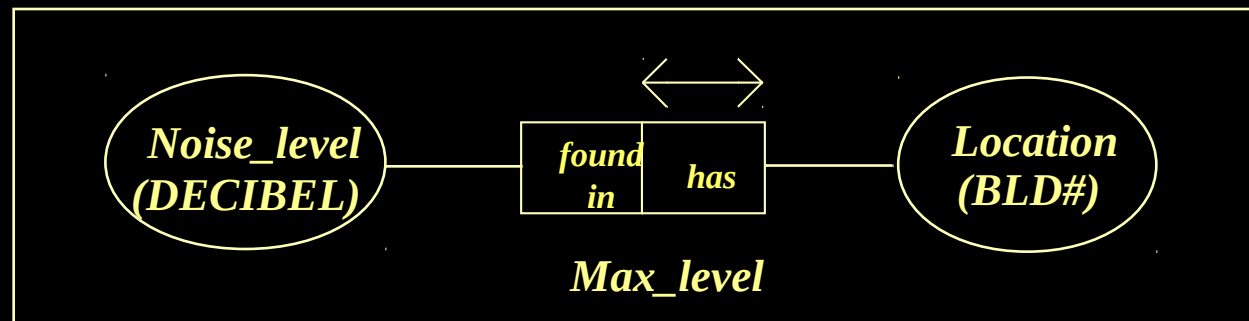


## TYPES AND INSTANCES

The failure of drawing the distinction between an entity type and an instance of an entity type is a common mistake.

Factory, Despatch and Reception are instances of an entity type. The fact type **Max\_level** occurs several times.

The correct schema should be:

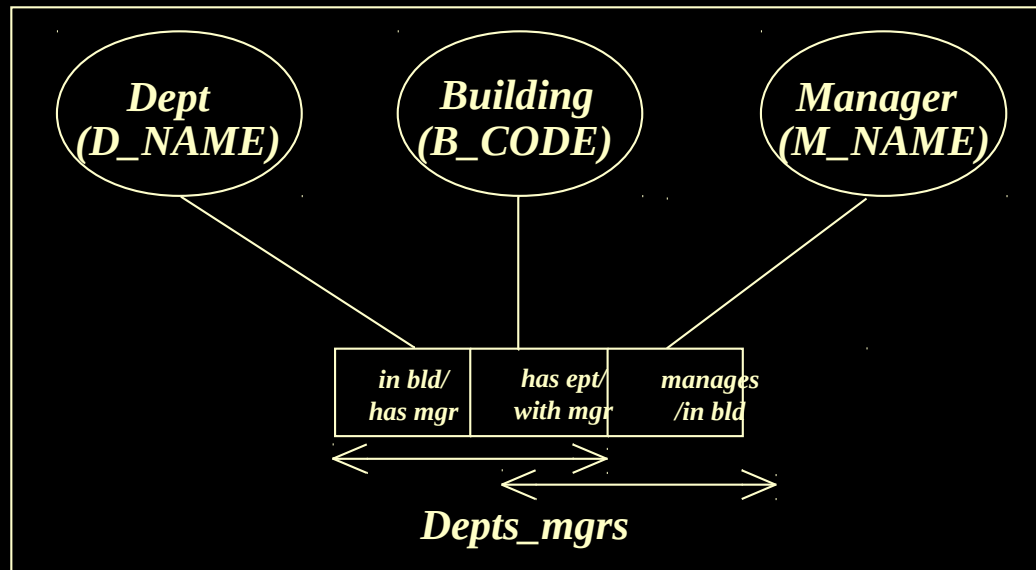


Let us consider a more complex example for UCons construction – remember the close relationship between the step 1 of the CSDP and configurations of Ucons.

## Example 1 Departments

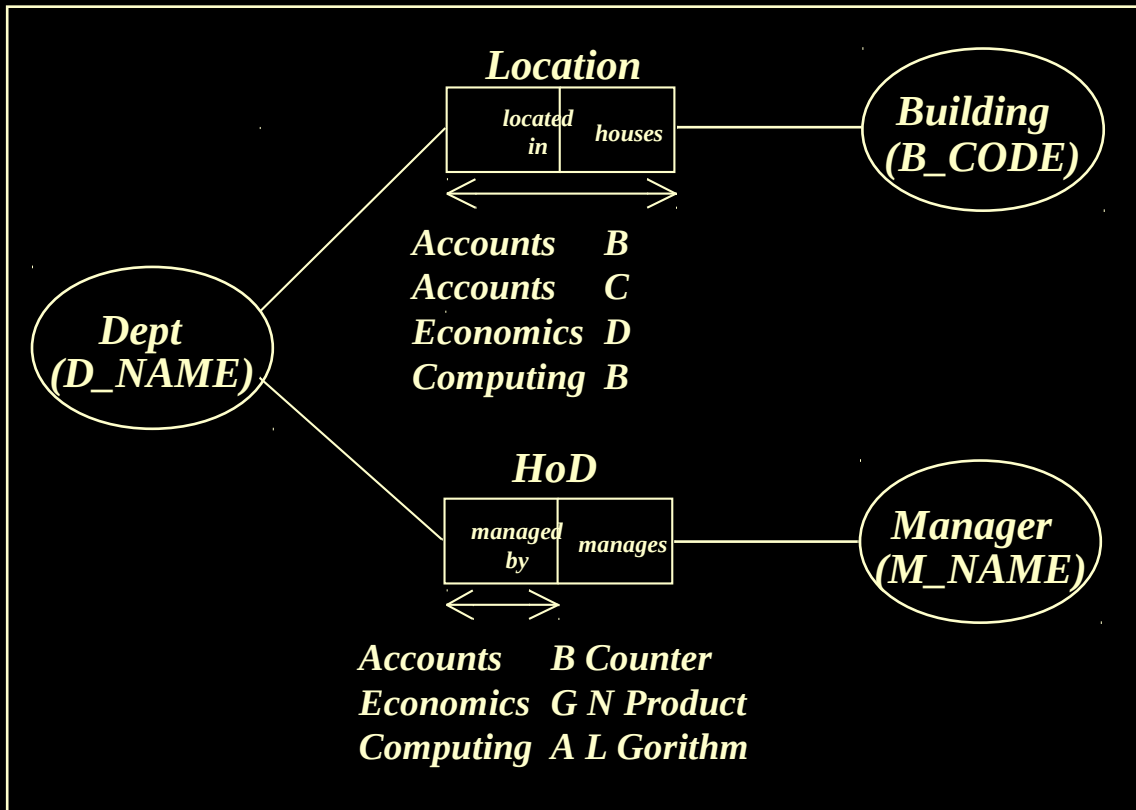
Notice the redundancy in this output report in all columns!!!

<i>Department</i>	<i>Building</i>	<i>Head of Dept</i>
<i>Accounts</i>	<i>B</i>	<i>B Counter</i>
<i>Accounts</i>	<i>C</i>	<i>B Counter</i>
<i>Economics</i>	<i>D</i>	<i>G N Product</i>
<i>Computing</i>	<i>B</i>	<i>A L Gorithm</i>



The schema is incorrect!

# The output report should be modelled as follows:



In this example, Dept, Building, and Manager are not all semantically related together.

Dept is associated with Building, and INDEPENDENTLY Dept is also associated with Manager.

Manager is 'partially' dependent on the pair (Dept, Building)

Shall we add one more Ucon for the fact type HoD?

The above schema containing 2 elementary fact types (with shown UCons) correctly represents the UoD illustrated by the output report.

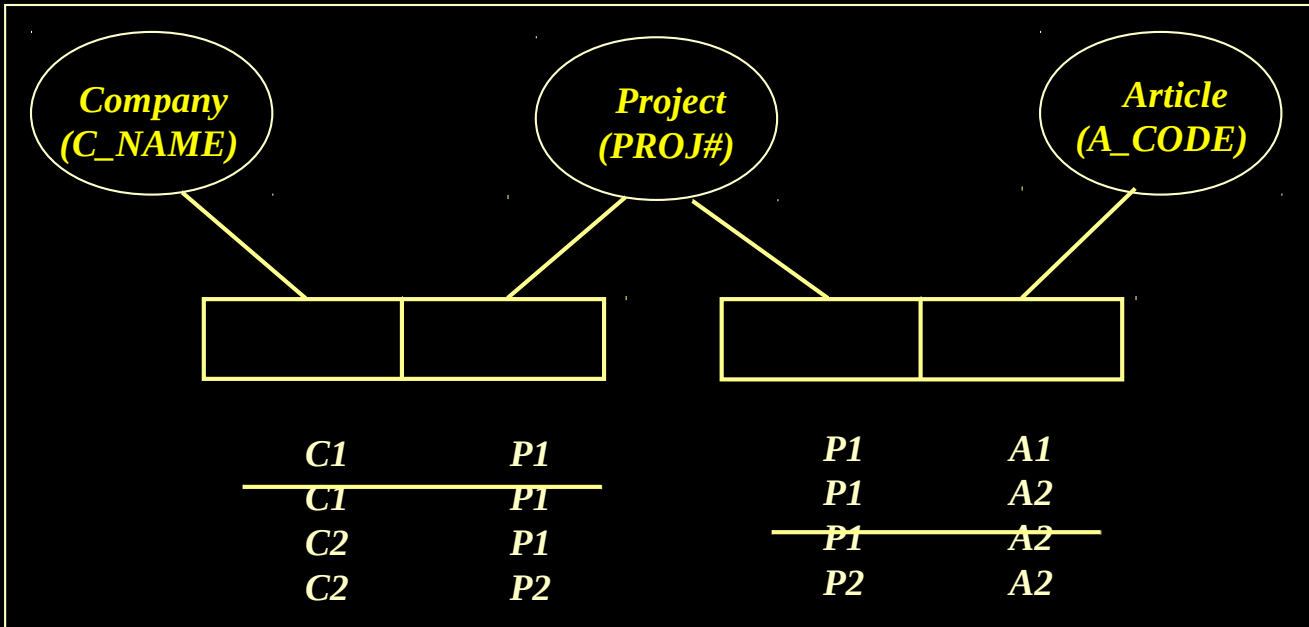
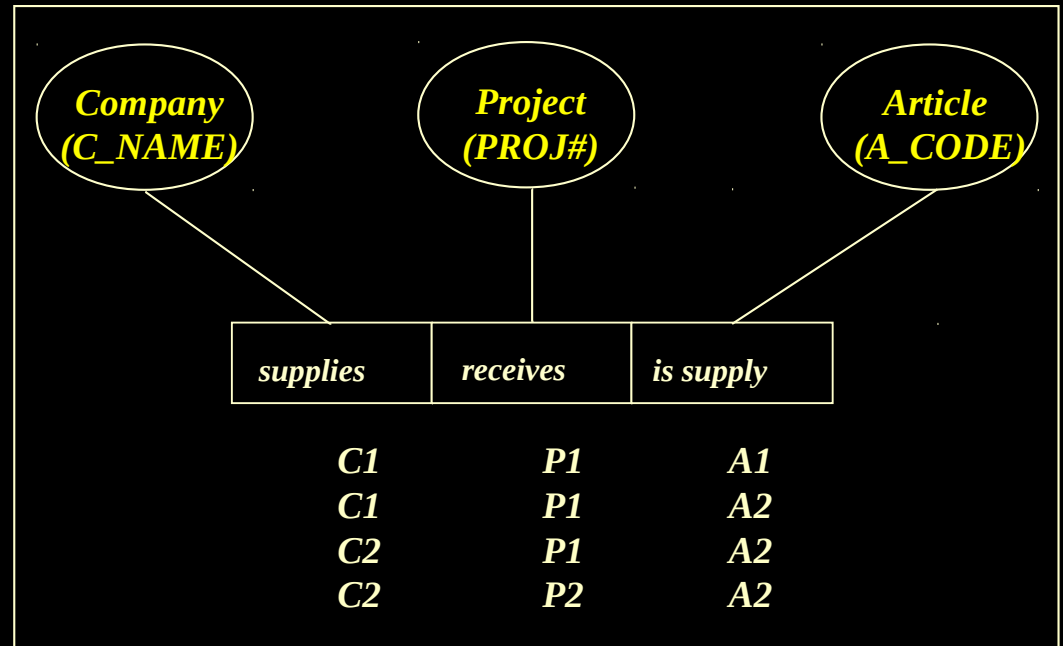
## Determine the length of elementary fact types:

**4A:** perform reducibility check, and if necessary, correct the conceptual schema diagram; the fact type was too 'long'.

**4B:** perform information loss check. Bring all the information of the output report into facts permitted by the conceptual schema and check that the original reports can be reconstructed without loss of information; the fact type was too restrictive.

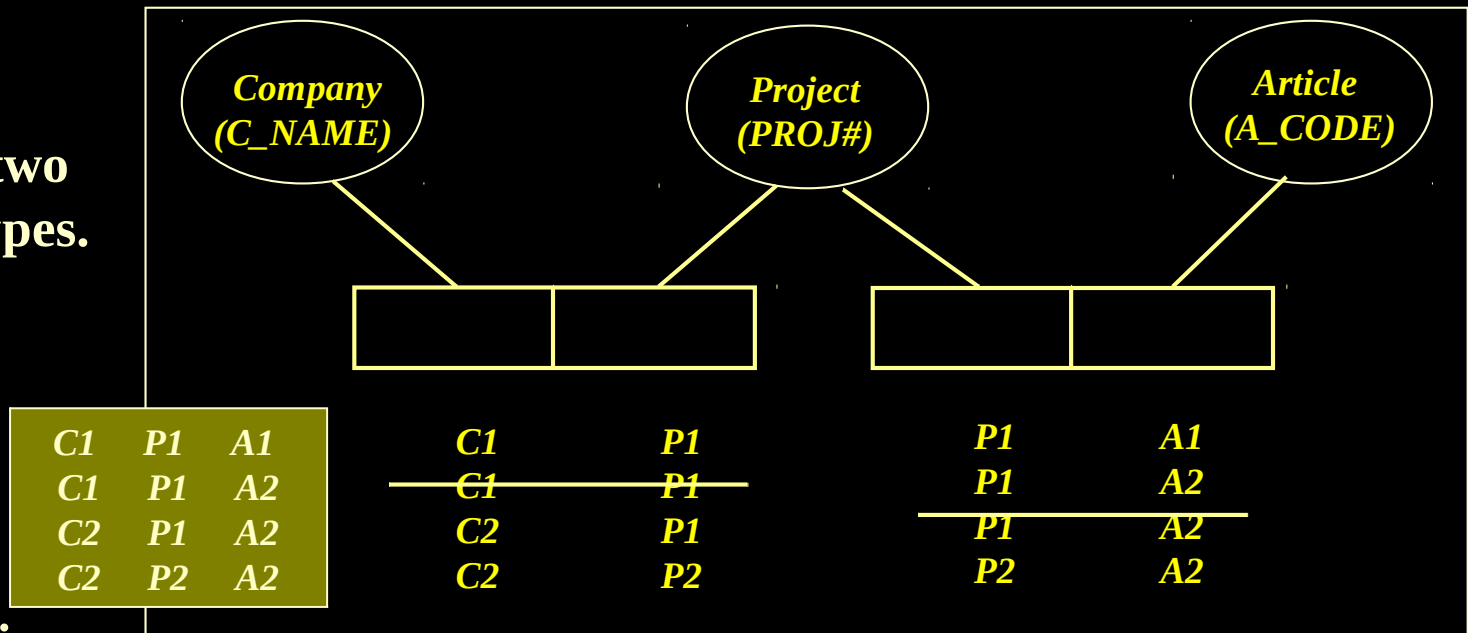
## Example 2 Project Needs

Splitting of this ternary fact type into two binary ones (on Project)

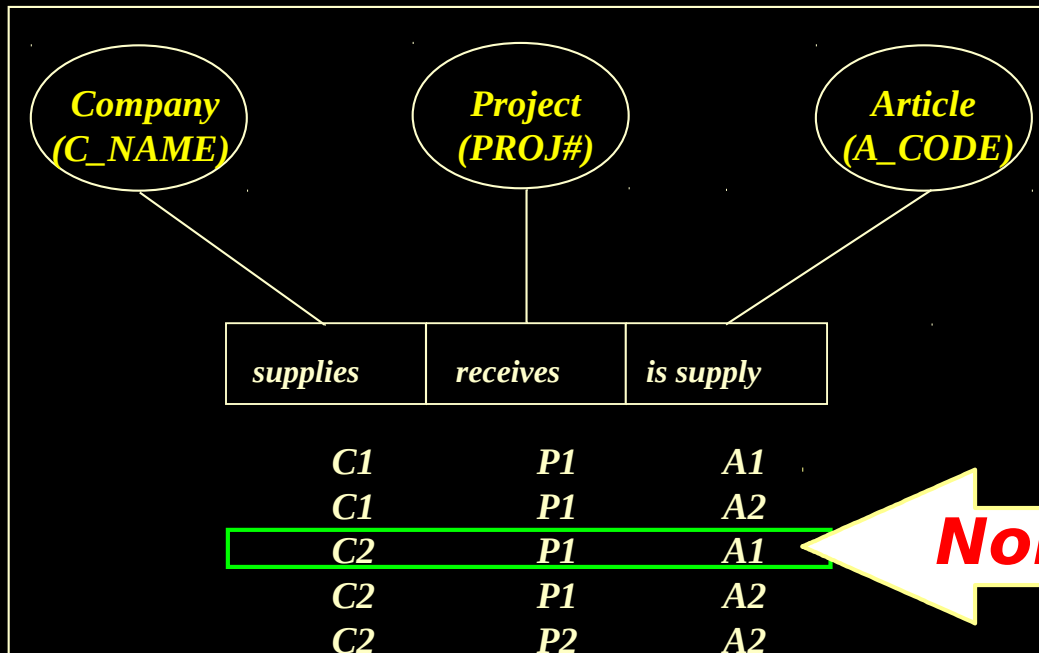


In this example, Company, Project, and Article are inter-related.

Grouping of two binary fact types.



After Join:

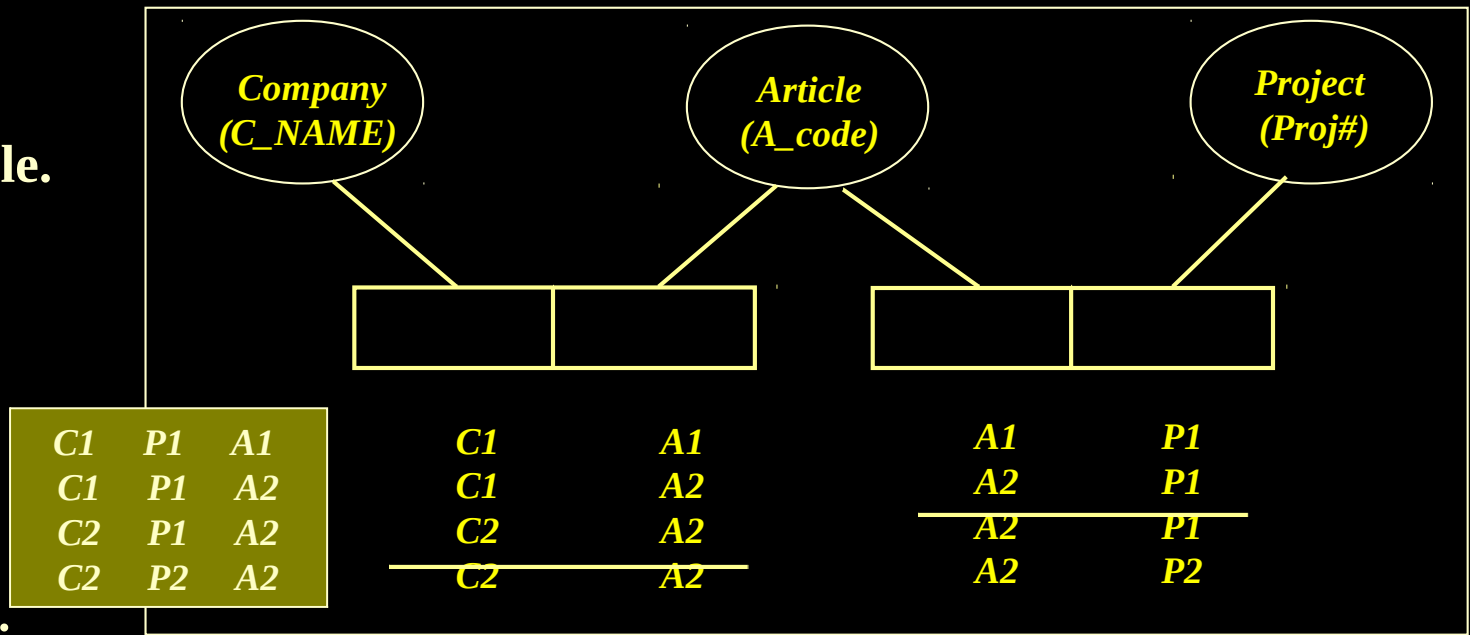


Conclusion:

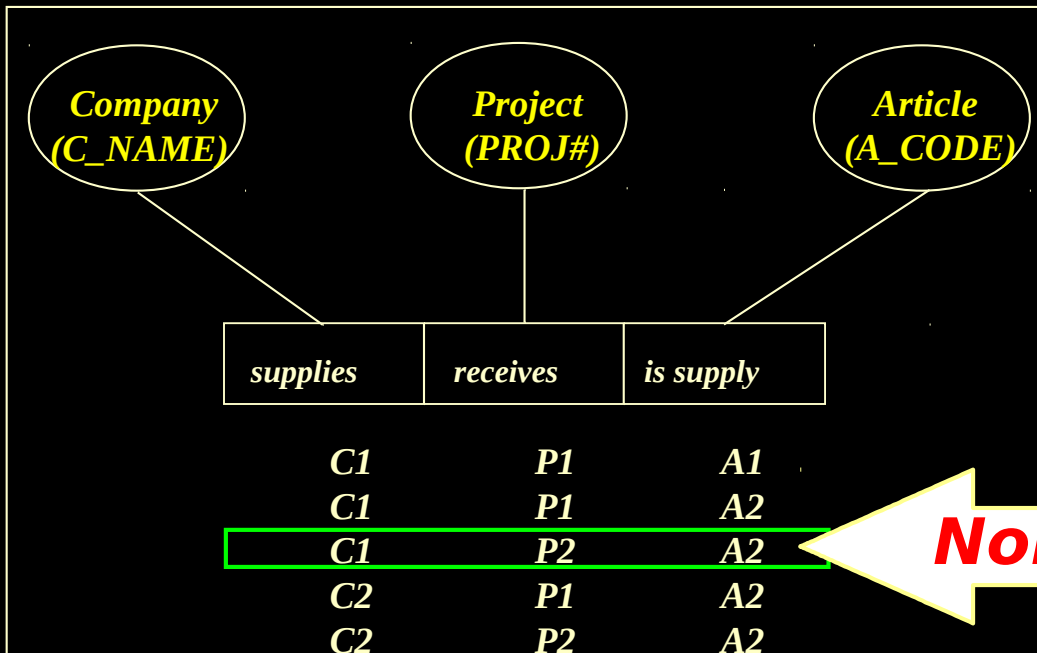
The ternary fact type **CANNOT** be split in the manner tried. Further splits should be tried: see next

**Non-fact**

Split on Article.



After Join:



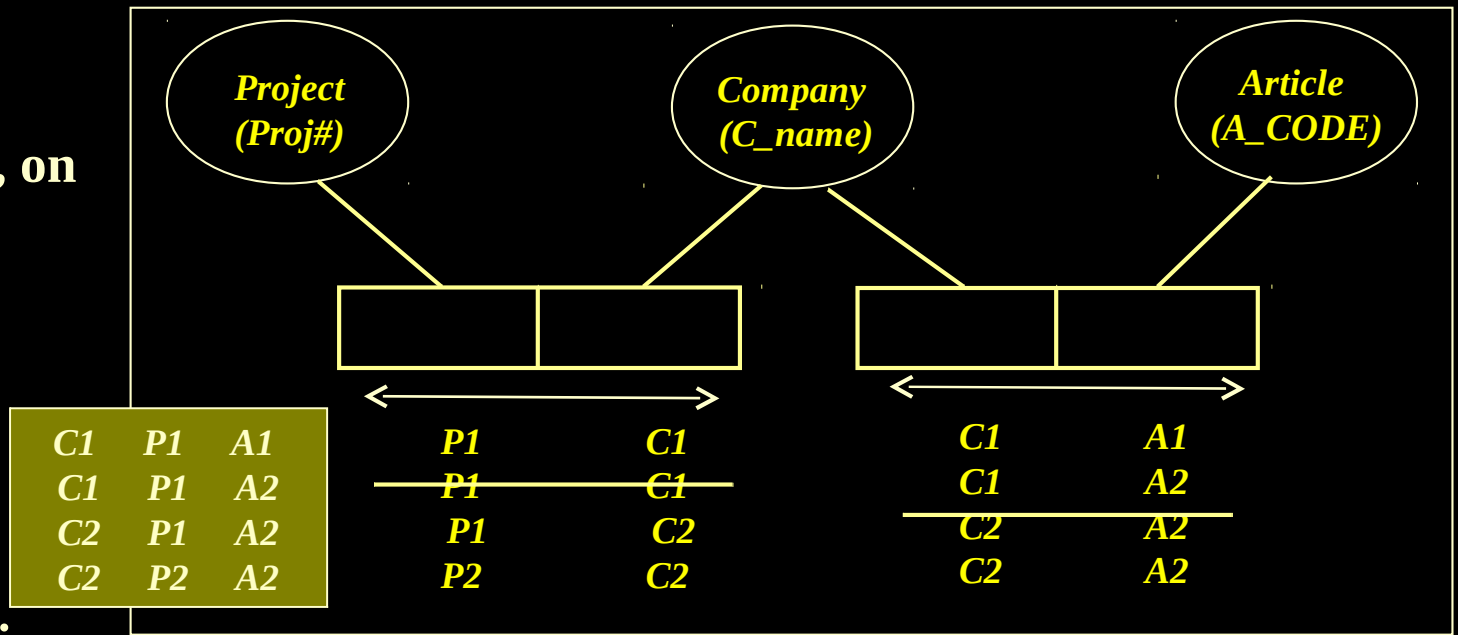
Conclusion:

Again, the ternary fact type **CANNOT** be split in the manner tried. Further splits should be tried: see next..

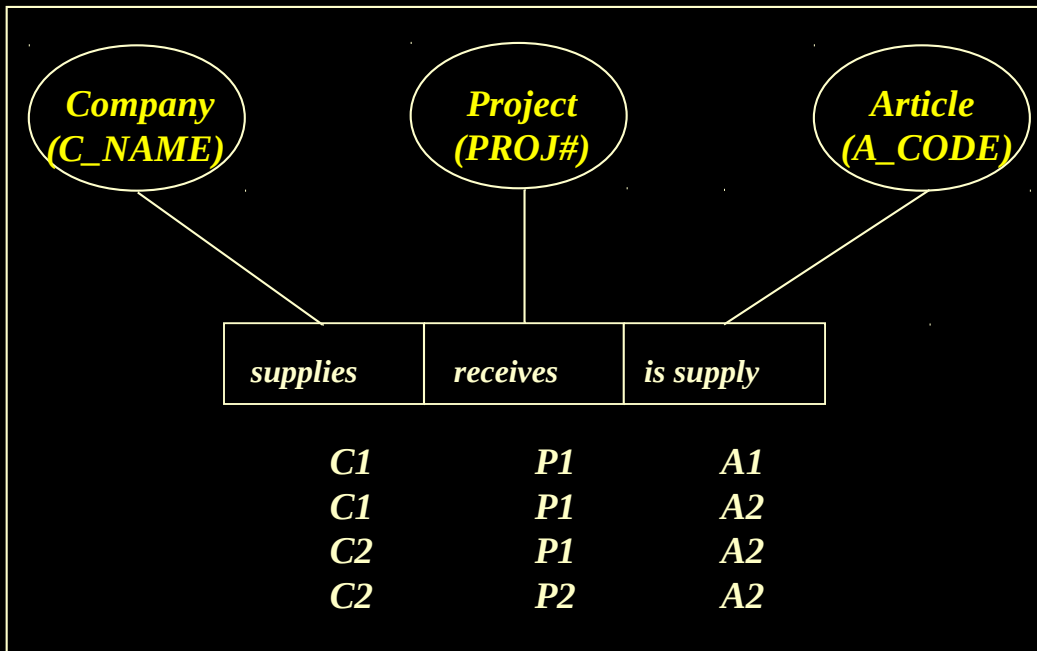
**Non-fact**



Another split, on Company.



After Join:



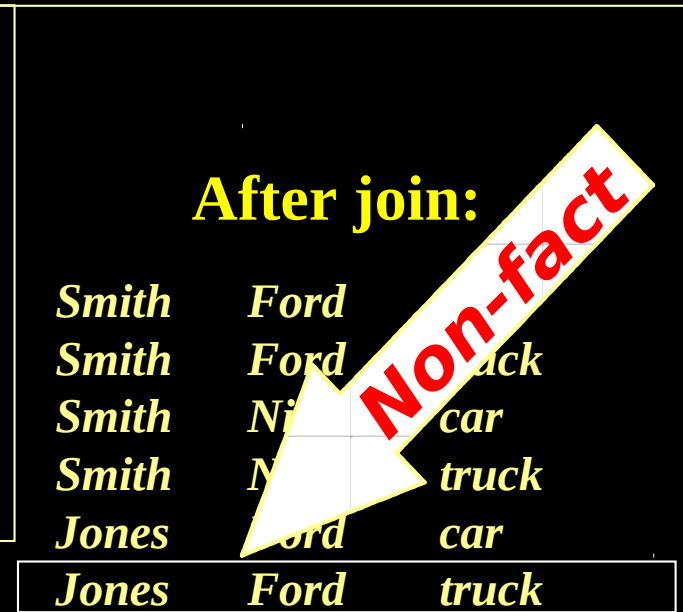
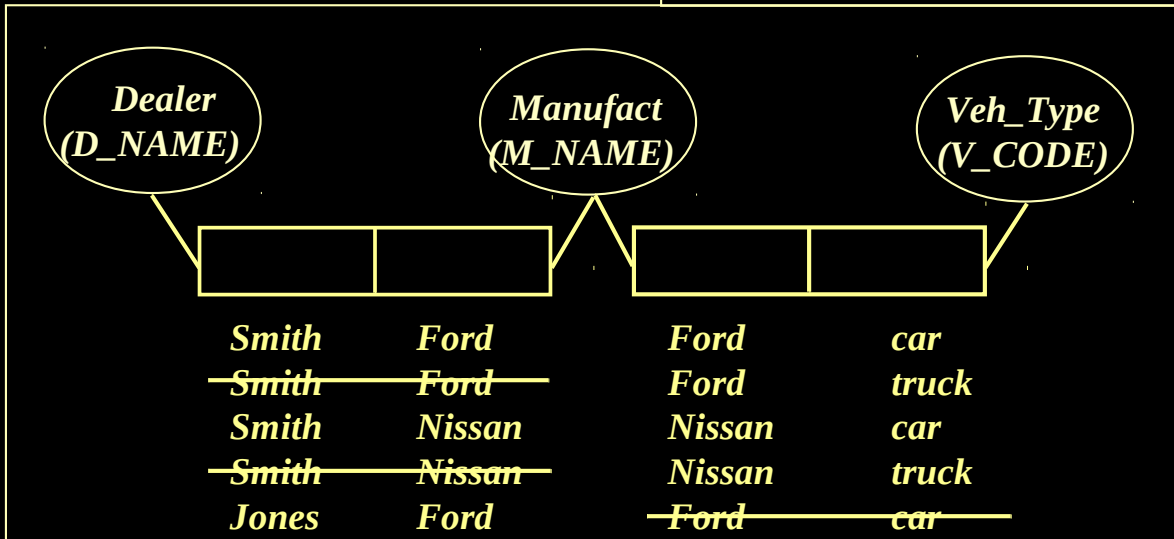
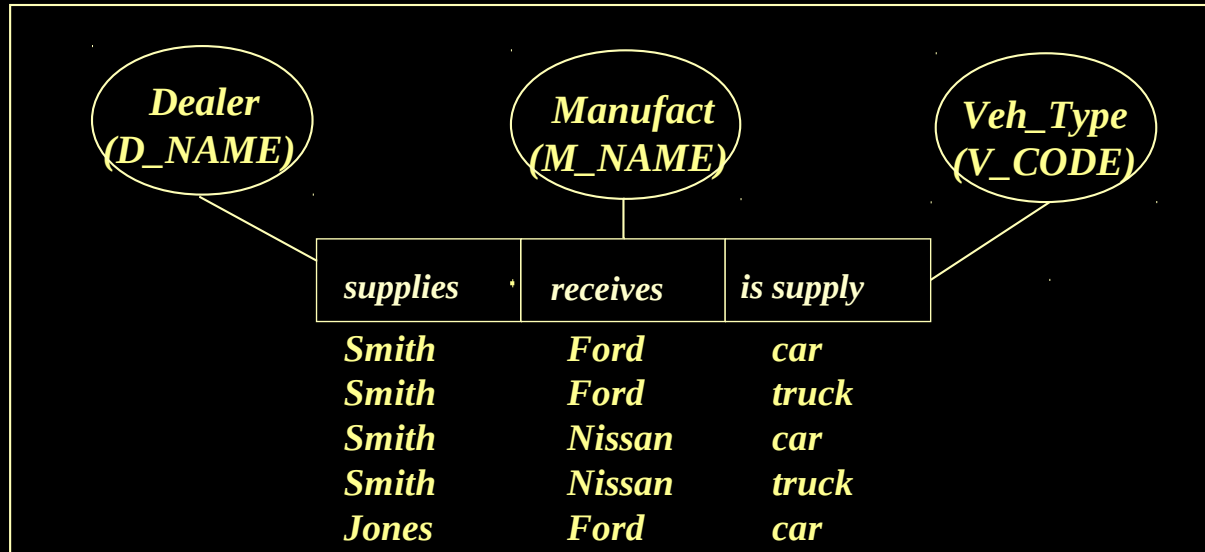
Join Produces original population

### Conclusion:

The ternary fact type CAN be split in the manner tried. No further splits should be tried in this case BUT WE MUST BE SURE about the data representativeness used for the splits

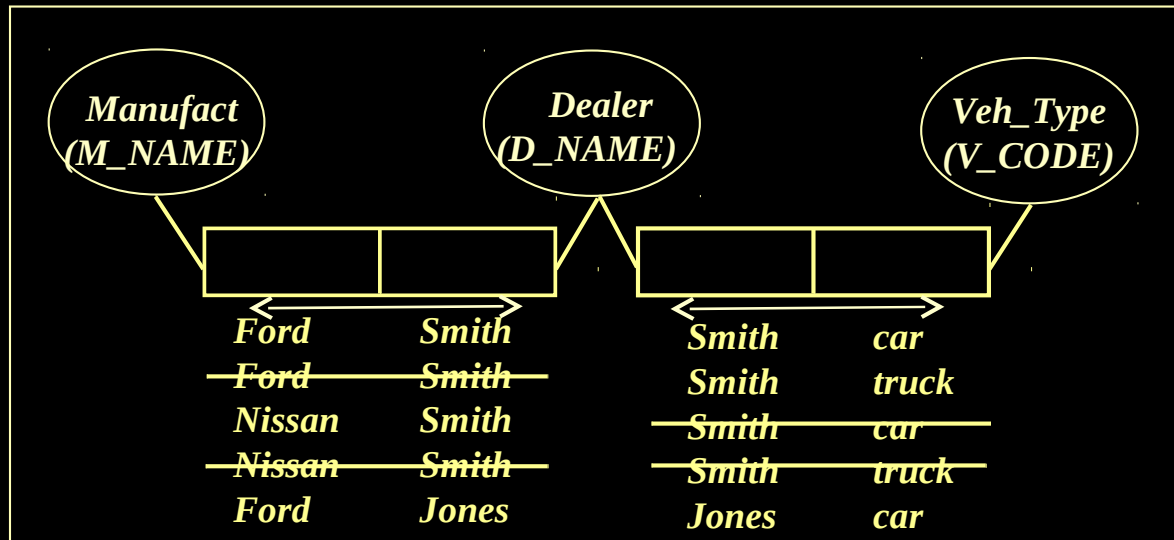
# Example 3: Dealers

Split and join  
(on manufacturer)



A non-fact has been generated.  
Therefore, this split is not correct!

## Consider another splitting possibility (there is a third one):



Join the two data samples:

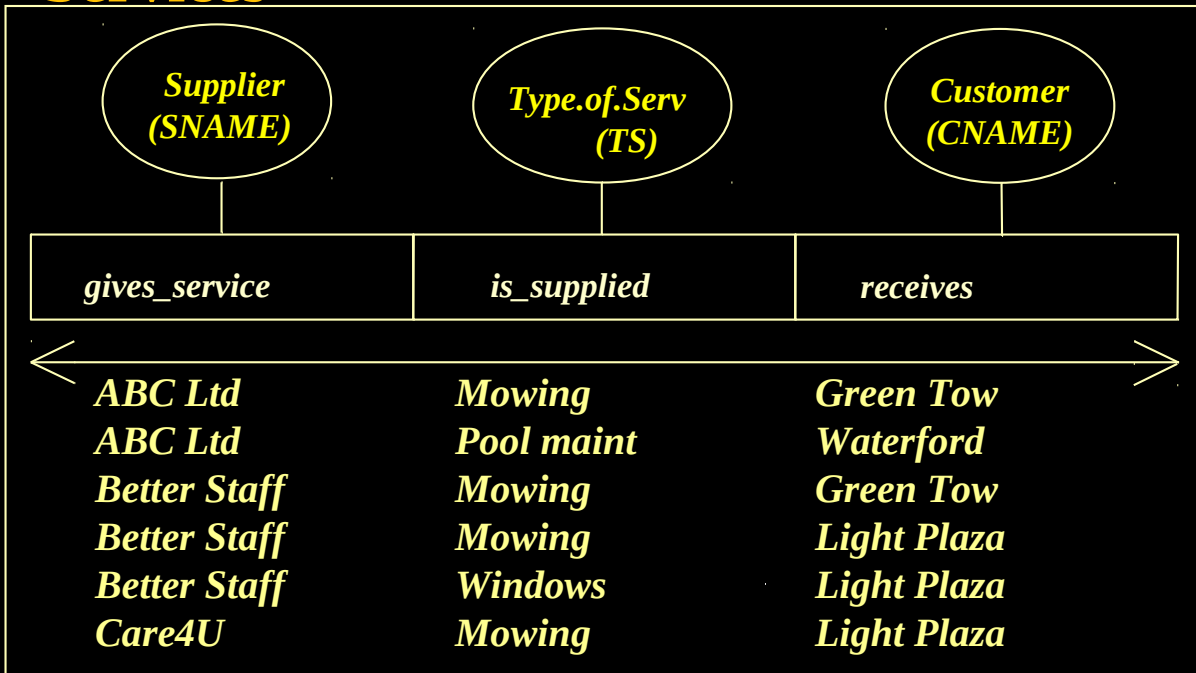
The original significant population has been recovered.

Therefore, the ternary is splittable on Dealer. This is an important result  
Redundancy is eliminated.

Smith	Ford	car
Smith	Ford	truck
Smith	Nissan	car
Smith	Nissan	truck
Jones	Ford	car

# Example 4:

## Services



## Projections

ST (Supplier – Type of service)

ABC Ltd	Mowing
ABC Ltd	Pool maint
<u>Better Staff</u>	<u>Mowing</u>
Better Staff	Mowing
Better Staff	Windows
Care4U	Mowing

SC

ABC Ltd	Green Tow
ABC Ltd	Waterford
Better Staff	Green Tow
<del>Better Staff</del>	<del>Light Plaza</del>
Better Staff	Light Plaza
Care4U	Light Plaza

TC

Mowing	Green Tow
<u>Pool maint</u>	<u>Waterford</u>
Mowing	Green Tow
Mowing	Light Plaza
<u>Windows</u>	<u>Light Plaza</u>
Mowing	Light Plaza

**Theoretically ALL COMBINATIONS** should be

tried before jumping to a conclusion:

1. (s,t) join (t,c), (split on t)
2. (s,t) join (s,c) (split on s) and
3. (t,c) join (s,c) (split on c)

Before attempting the three way join

4. (s,t) join (t,c) join (s,c).

# Joins of any two tables differ from the original output report .

**ST Join SC:**

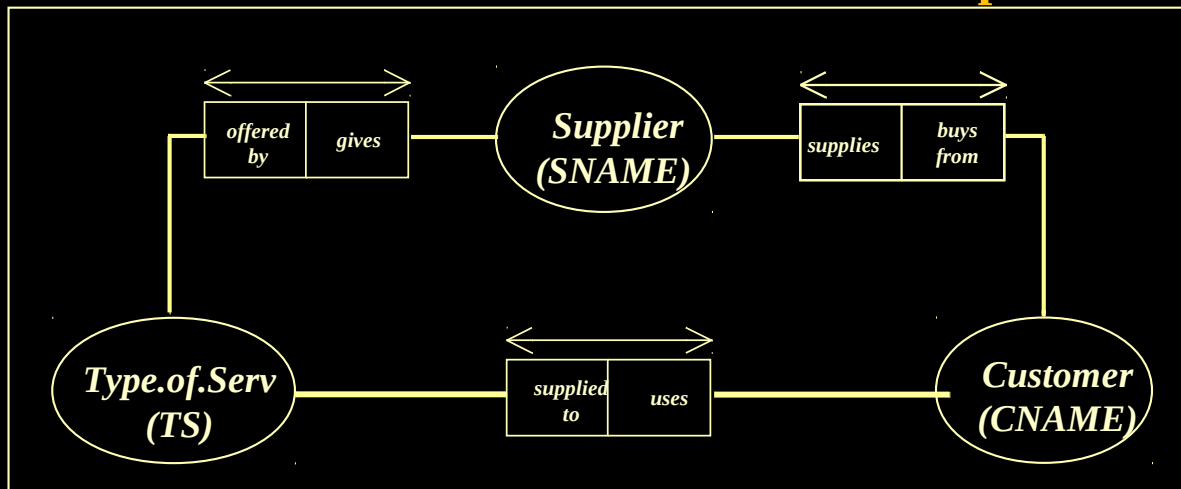
ABC Ltd	Mowing	Green Tow
ABC Ltd	Mowing	Waterford
ABC Ltd	Pool maint	Green Tow
ABC Ltd	Pool maint	Waterford
Better Staff	Mowing	Green Tow
Better Staff	Mowing	Light Plaza
Better Staff	Windows	Green Tow
Better Staff	Windows	Light Plaza
Care4U	Mowing	Light Plaza

**(ST Join SC) Join TC:**

ABC Ltd	Mowing	Green Towers
ABC Ltd	Pool maint	Waterford
Better Staff	Mowing	Green Towers
Better Staff	Mowing	Light Plaza
Better Staff	Windows	Light Plaza
Care4U	Mowing	Light Plaza

**Original  
table**

**The original population is recovered from the three binary fact types. The correct schema is shown below to replace the 3-ary fact type on slide 20.**



## ***IMPORTANT OBSERVATIONS!!!!***

*Even though an n-ary fact type should have a uniqueness constraint spanning at least n-1 roles it may be splittable into several smaller fact types.*

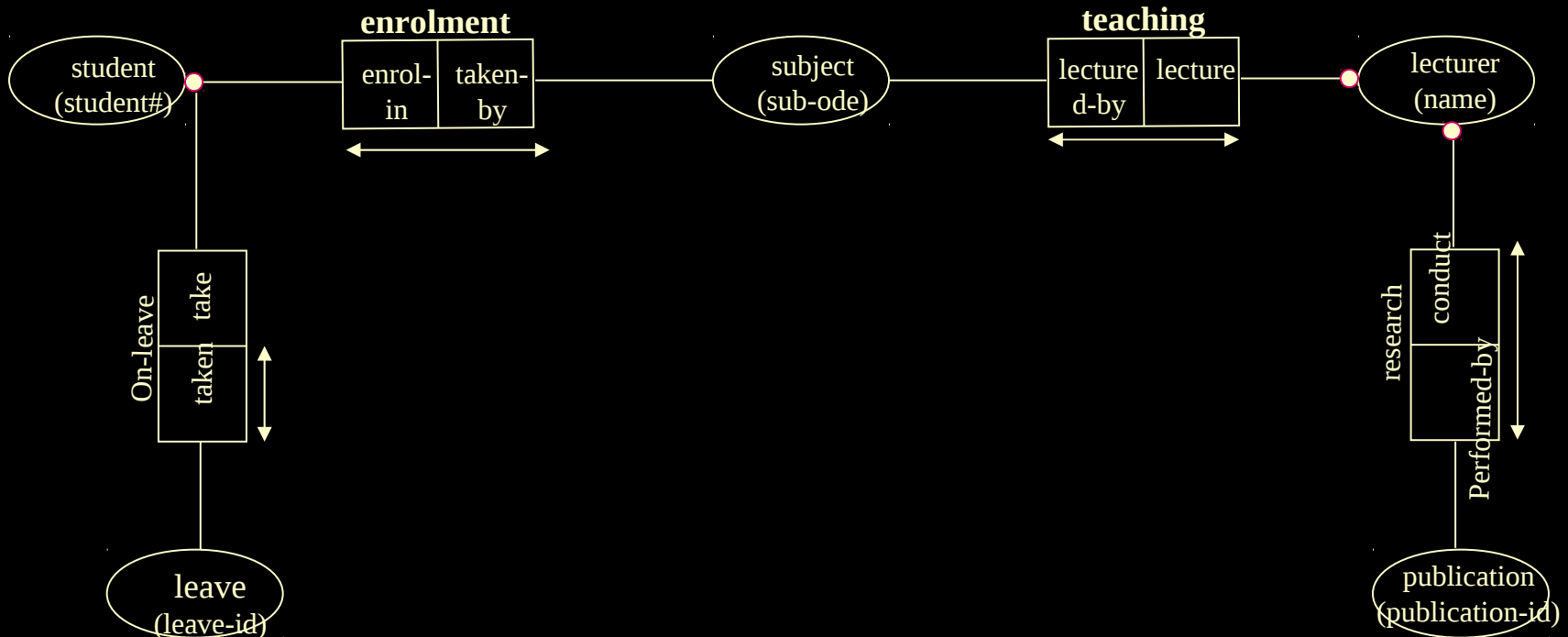
*All possible splits have to be considered before a fact type can be considered unsplittable. In practice the analysis should be simplified by designer understanding of terms and relationships in the considered UoD.*

## ***Advices and summary for beginners:***

- 1. You only model semantically inter-related entities ( $N \geq 3$ ) as ternary or higher order fact types;**
- 2. Refine your model by the splitability check;**
- 3. In real life UoDs we might have higher order fact types present. So we should be able to identify them;**
- 4. Nested FT is useful when it participates in another non-nested FT(s). Otherwise there is no need to use it. So, use nesting with care!**

# Step 5 - Add mandatory role constraint – (each instance of an entity **MUST** participate in the role)

**Example :** Each lecturer must conduct teaching *and* research.  
 A student is either enrolling in subjects *or* on-leave.



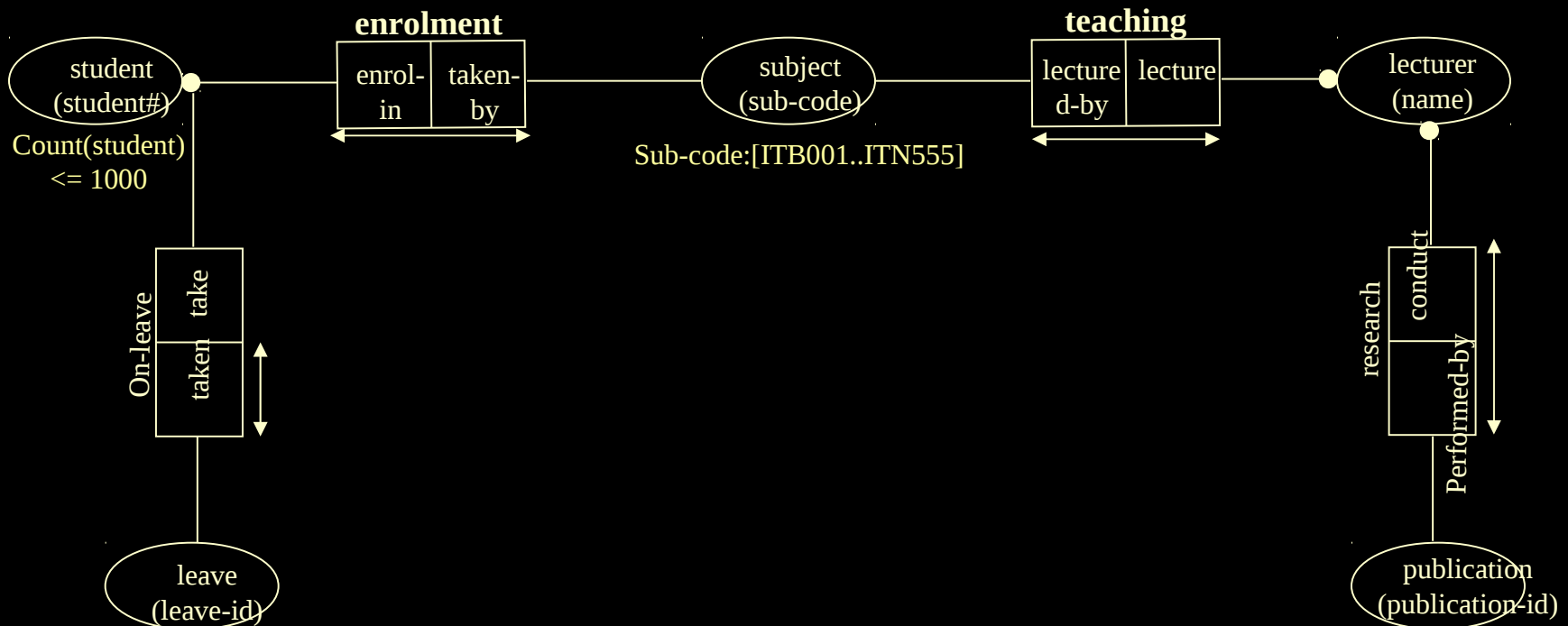


## Step 5 (con't)

### 2. Add cardinality entity/label constraints.

**Entity constraint:** No. of students is less than or equal to one thousand.

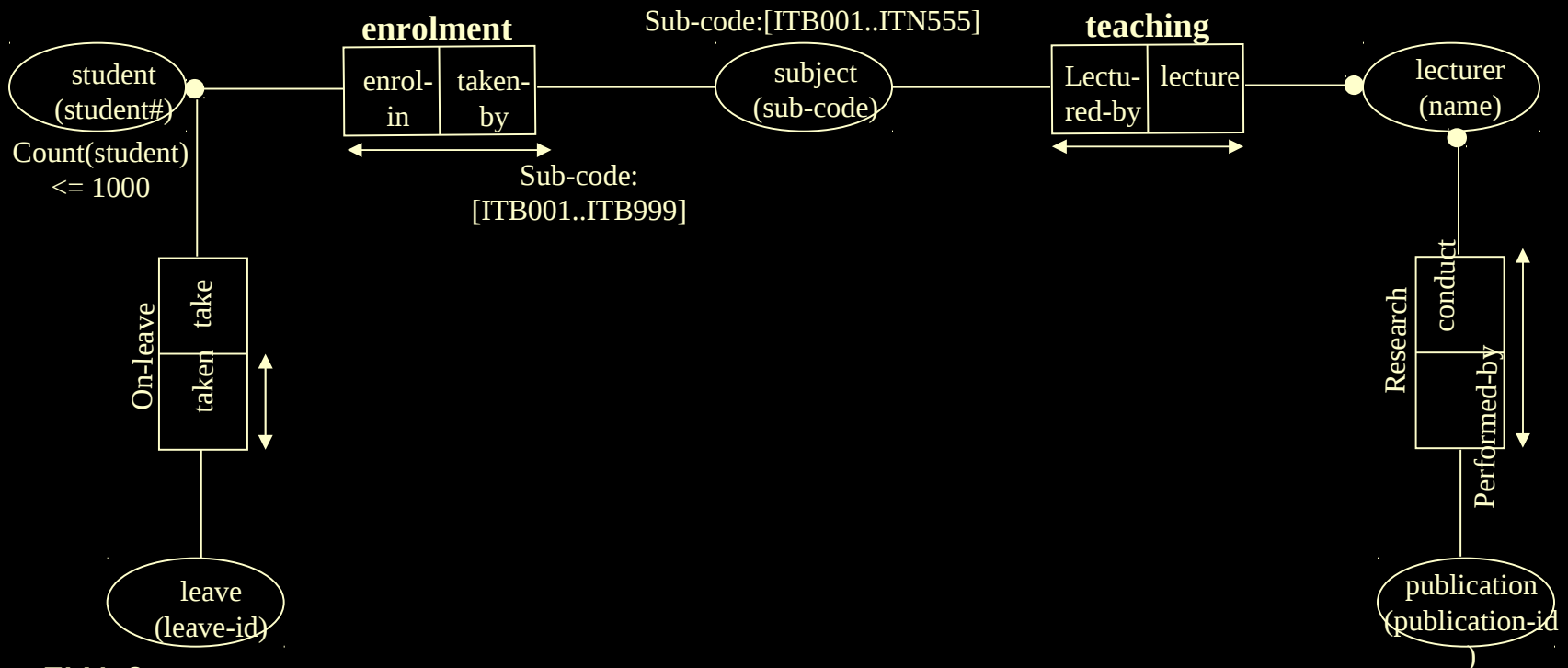
**Label constraint:** Valid subject codes are between ITB001 and ITN555.



## Step 5 (con't)

### 3. Add role constraints.

**Role constraint: Only subjects with subject-codes between ITB001 and ITB999 can be taken by students.**

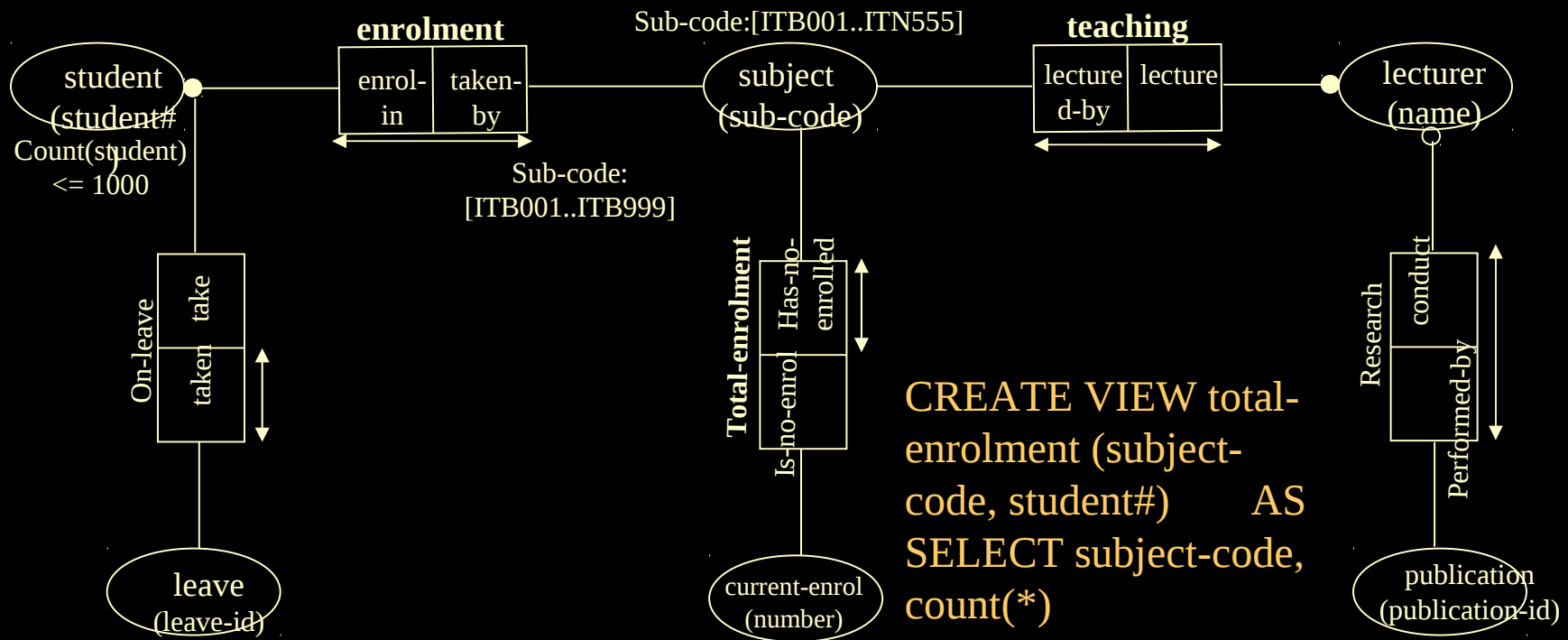


## Step 5 (con't)

### 4. Check logical derivation.

The **total-enrolment** fact type can be derived from other facts:

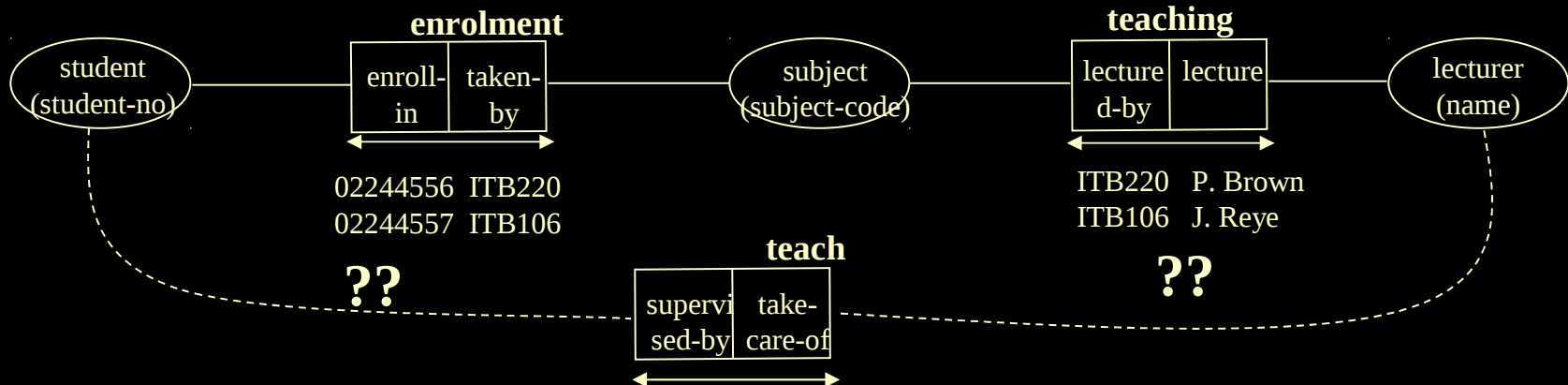
*Therefore, total-enrolment should be removed at Step 5!*



## Step 5 (con't)

Is the TEACH fact type logically derived from the the teaching fact type and enrolment fact types?

**Answer: Yes. So, it should be deleted from the conceptual schema. However, if a supervision relationship (e.g. thesis supervision) exists independent of normal teaching (course-work) relationship, a thesis-supervision fact type may be added.**

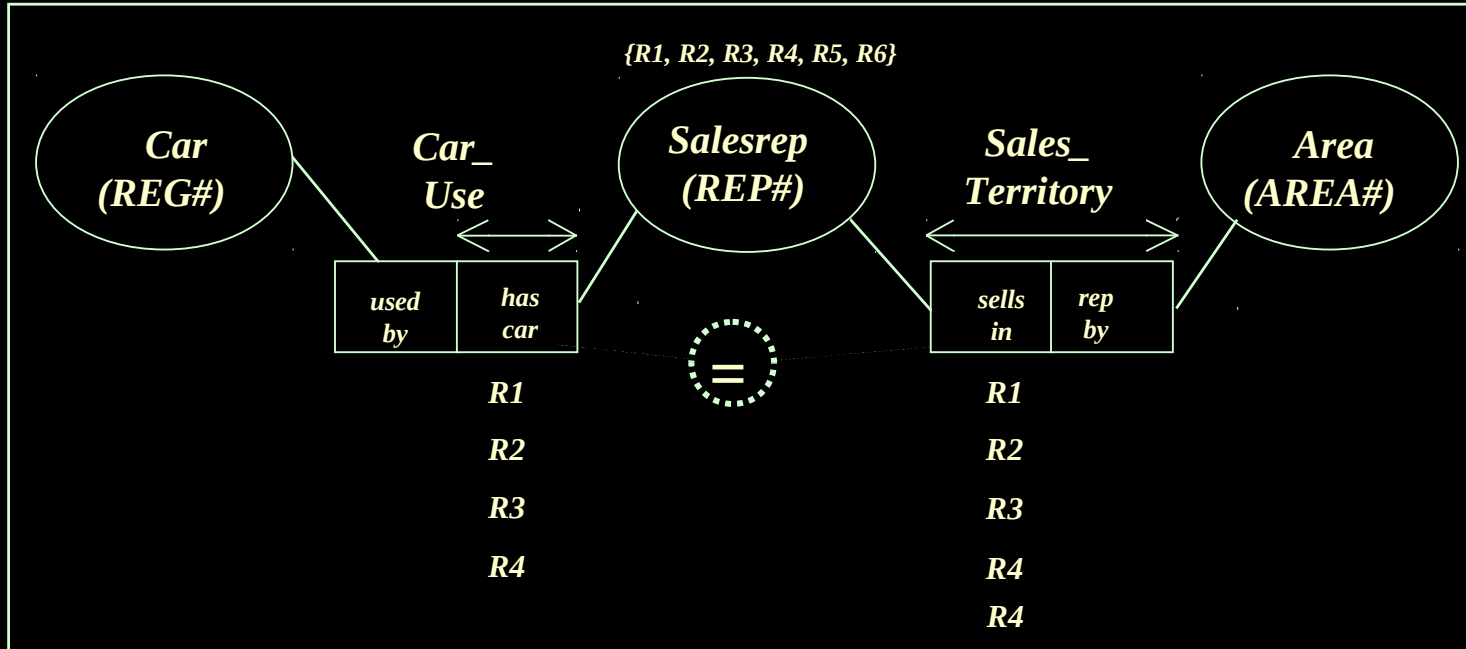


# Step 6 - Set Constraints

## Equality constraint - SET EQUALITY

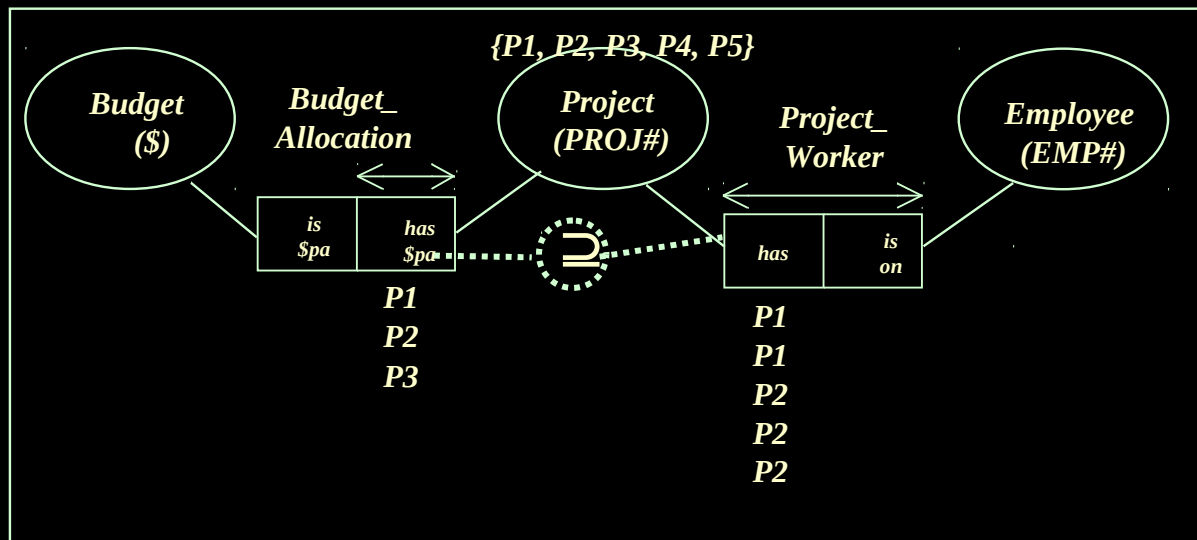
The set of entity instances involved in one role is exactly the same as a set of the entity instances involved in a second role.

### Example



## Subset constraint

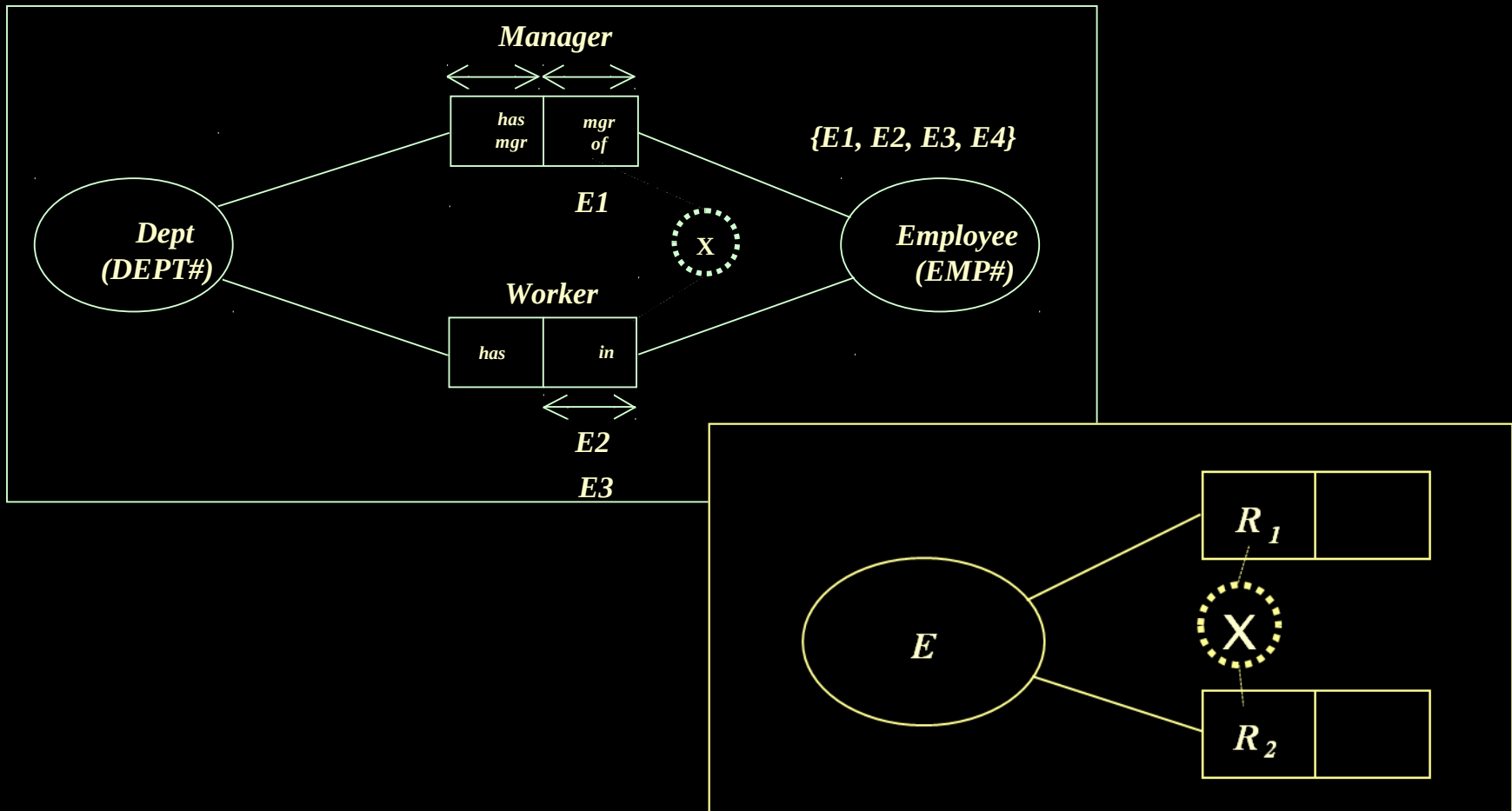
The set of entity instances involved in one role is a subset of the entity instances involved in a second role.



Each Project that can employ workers must have a budget; some of these project can have no a worker allocated yet, but other projects can have many workers allocated.

## Exclusion constraint

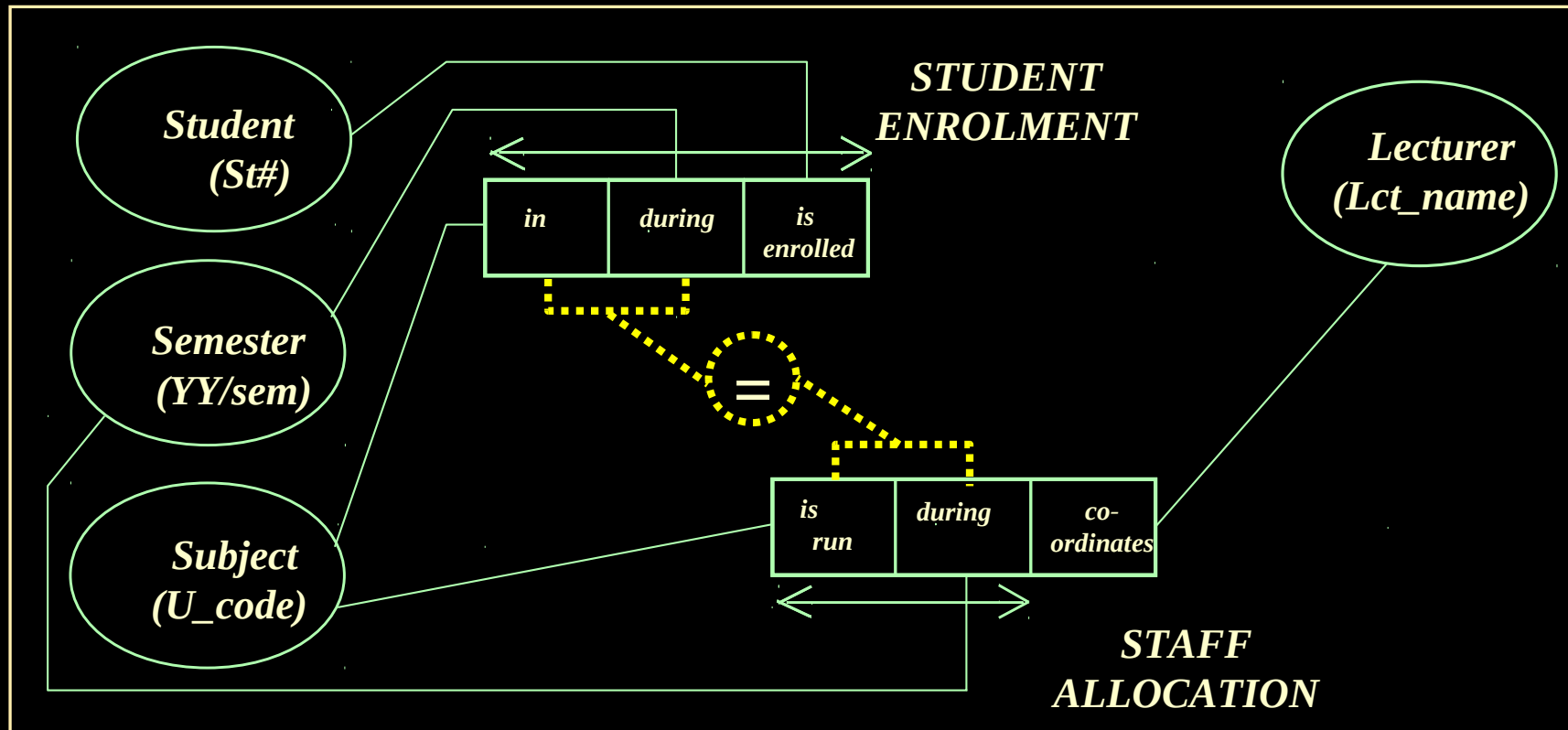
If an entity instance is involved in one role it is excluded from involvement in another role.



## Multiple-role Equality constraint

The set of combinations of entity instances of two or more entity types involved in two fact types are exactly the same.

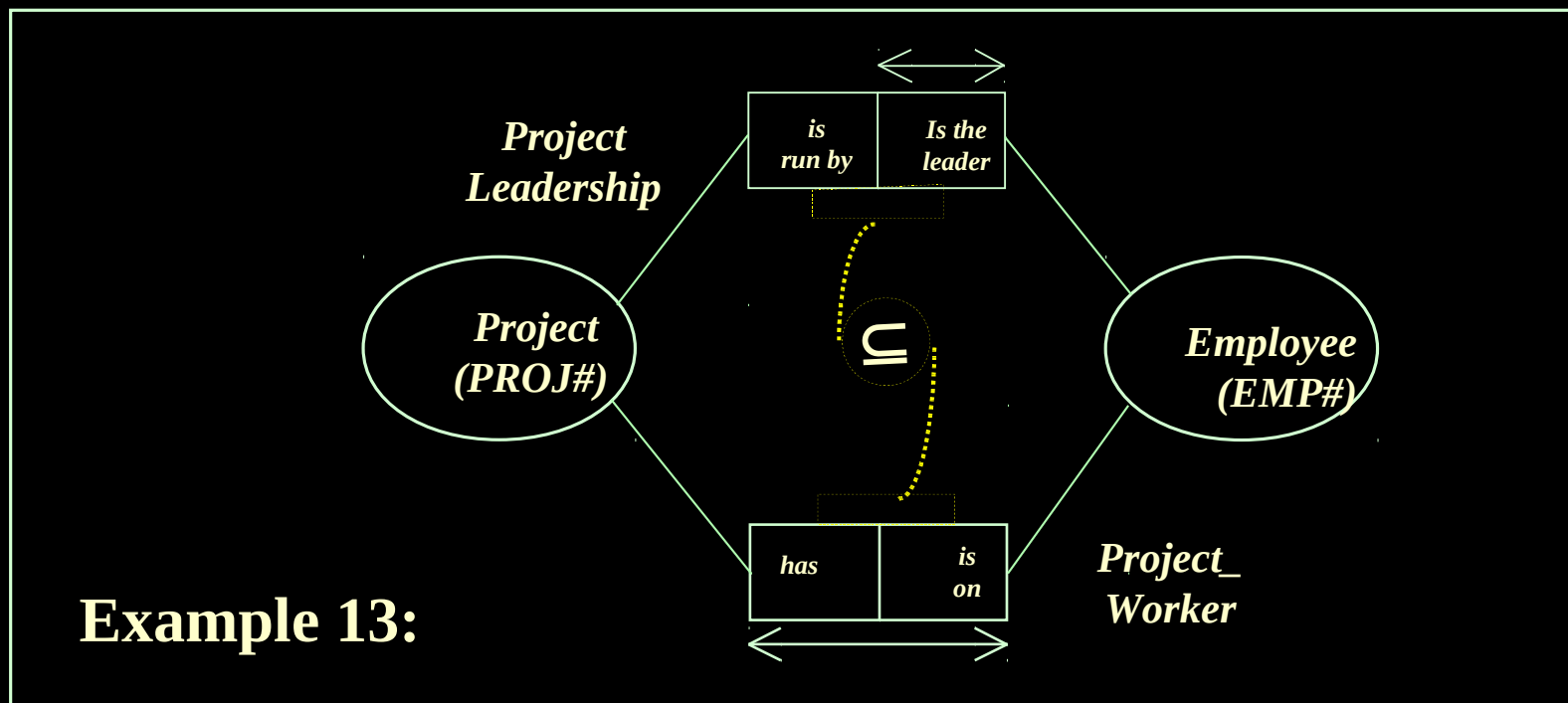
### Example 12





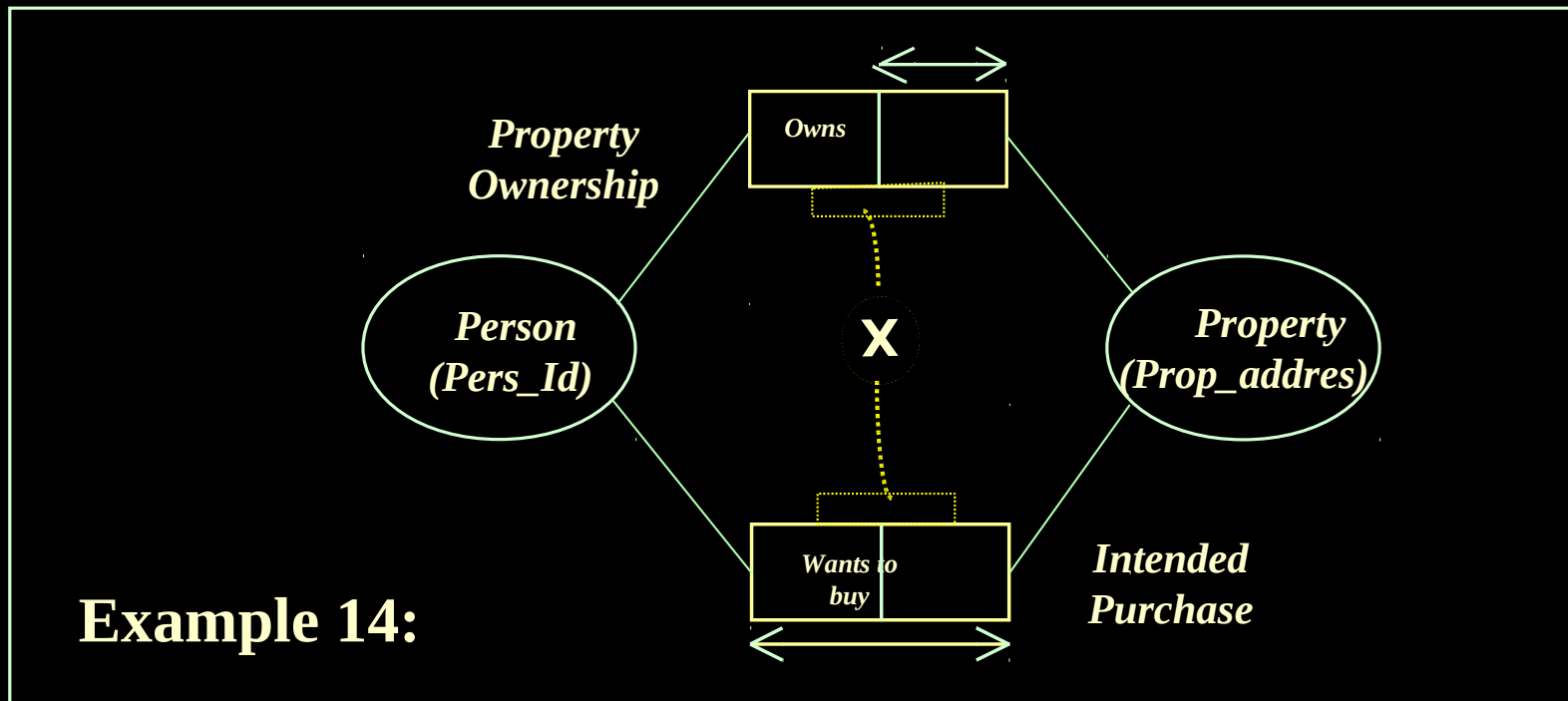
## Multiple-role Subset constraint

The sets of combinations of entity instances of the same entities involved in two fact types are in a inclusion relationship.



## Multiple-role Exclusion constraint

The sets of combinations of entity instances of the same entities involved in two fact types are in an exclusion relationship.



## General definitions (more formal)

Consider two Fact Types  $F$  and  $F'$  that have subsets of their roles

$$R = \{R_{k1}, R_{k2}, \dots, R_{km}\} \text{ and } R' = \{R'_{h1}, R'_{h2}, \dots, R'_{hm}\}$$

where in each pair of corresponding roles  $R_{ki}$  and  $R'_{hi}$  ( $i=1..m$ ) are defined on the same entity type. We say that these sets of roles satisfy a set constraint, if the population of any instance of the fact type  $F$  restricted to the set  $R$  of roles,  $\text{pop}(R)$ , is involved in the same set\_relationship with the population of  $F'$  restricted to  $R'$ ,  $\text{pop}(R')$ . In particular;



Fact types  $F$  and  $F'$  satisfy equality constraint on  $R$  and  $R'$  if for any instance of the UoD  $\text{pop}(R) = \text{pop}(R')$



Fact types  $F$  and  $F'$  are involved in the subset constraint on  $R$  and  $R'$  if for any instance of the UoD  $\text{pop}(R) \subseteq \text{pop}(R')$



Fact types  $F$  and  $F'$  are involved in the exclusion constraint on  $R$  and  $R'$  if for any instance of the UoD  $\text{pop}(R) \cap \text{pop}(R') = \emptyset$  (are disjoint)

## Example to illustrate complex configurations of constraints.

The first purpose of the presented example is to show how the set constraints could be identified from the rules valid in a larger domain. The other purpose is to identify a possibly complete set of constraints that will guarantee the consistency of data with the rules that must be enforced in the particular domain. The example is concerned with the UOD ‘Tennis tournaments’. For simplicity we consider only data from one year and we introduce limitation to cover only events from one stream (say men singles) and from quarter-finals upwards.

The rules of any tournament organisation are well known. Two players play a match and the winner advances to the next level. No other players than winners in Quarter-final and Semi-finals, can play in Semi-finals and Final of a given tournament respectively. To check if the set of constraints on the schema is sufficient to enforce consistency of data with the rules of the UoD, we may introduce an amendment of the output report by some corrupted data that violate UOD rules but satisfy constraints that are introduced so far. We will identify the constraint(s) that could prevent presence of such data.

The abbreviations used are;

Q, S, F (in the column Lev(el)) – Quarter-final, Semi-final, Final

A, B, C, ....(in the columns Win(ner), Los(er)) – Synonyms for Player Ids

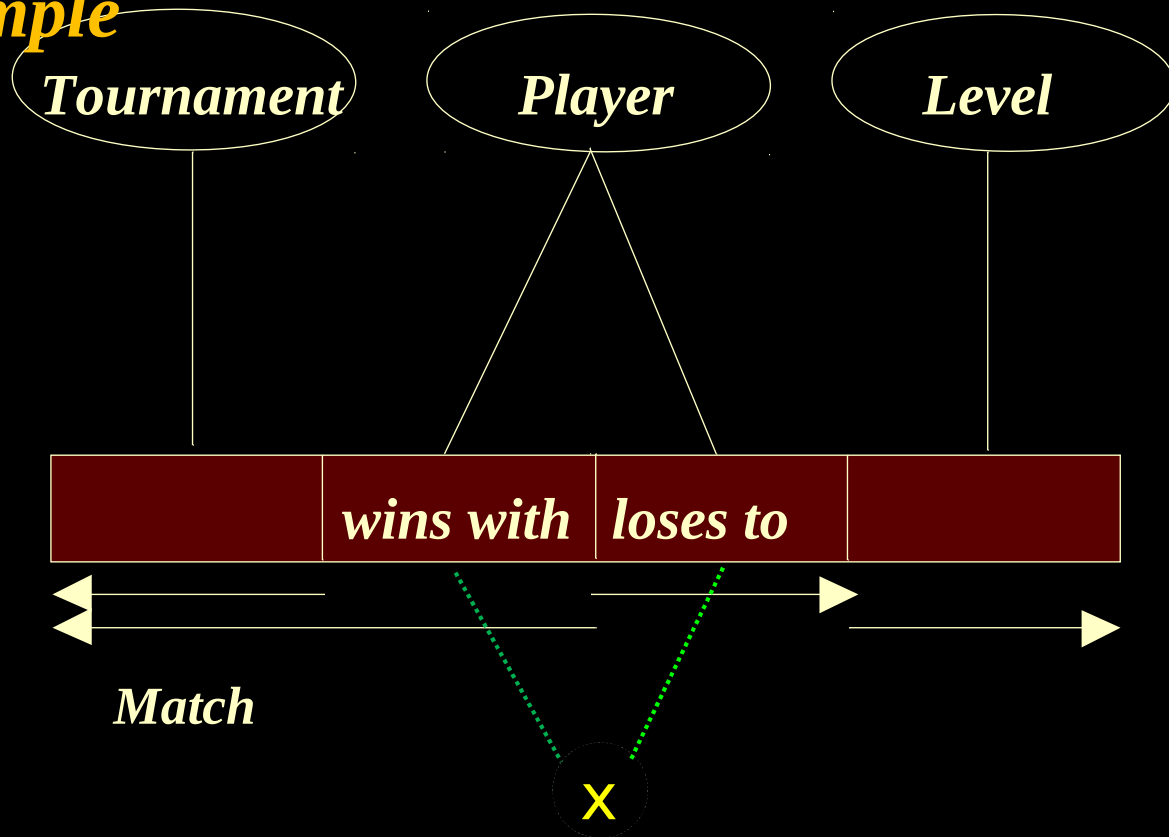
Wi, AO – examples of tournament shortened names (Wimbledon, Australia Open)

# Set Constraints – Example

## Tennis Tournaments

<i>Tour</i>	<i>Lev</i>	<i>Win</i>	<i>Los</i>
<i>Wi</i>	<i>Q</i>	<i>A</i>	<i>H</i>
<i>Wi</i>	<i>Q</i>	<i>B</i>	<i>G</i>
<i>Wi</i>	<i>Q</i>	<i>C</i>	<i>F</i>
<i>Wi</i>	<i>Q</i>	<i>D</i>	<i>E</i>
<hr/>			
<i>Wi</i>	<i>S</i>	<i>A</i>	<i>D</i>
<i>Wi</i>	<i>S</i>	<i>B</i>	<i>C</i>
<hr/>			
<i>Wi</i>	<i>F</i>	<i>A</i>	<i>B</i>
<hr/>			
<i>AO</i>	<i>Q</i>	<i>B</i>	<i>D</i>
<i>AO</i>	<i>S</i>	<i>D</i>	<i>J</i>

For simplicity, label types are omitted here.



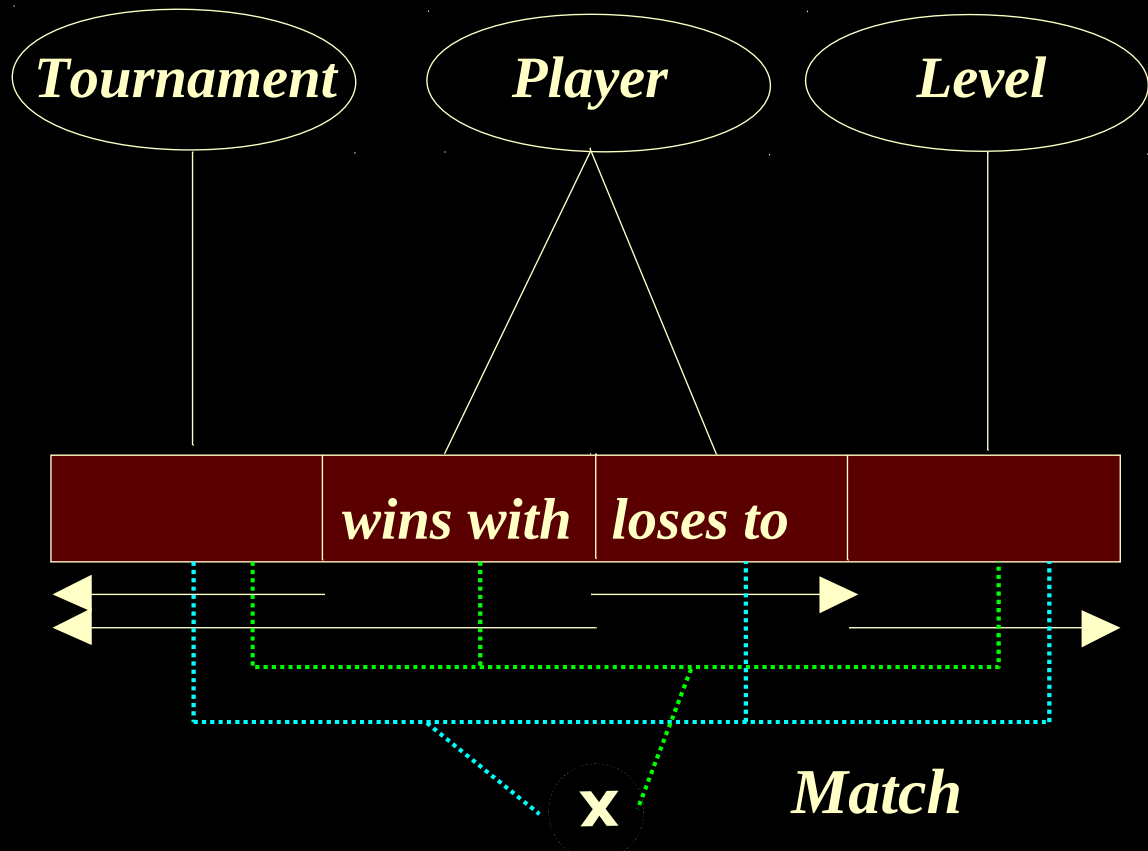
1. During any tournament one can be defeated only once

2. During any tournament one can win only once in any stage (Q,S,F)

Is the exclusion constraints valid for this UoD?  
Obviously NOT.

# Tennis Tournaments

Tour	Lev	Win	Los
Wi	Q	A	H
Wi	Q	B	G
Wi	Q	C	F
Wi	Q	D	E
-----			
Wi	S	A	D
Wi	S	B	C
Wi	F	A	B
-----			
Ao	Q	B	D
Ao	S	D	J
-----			
.....			



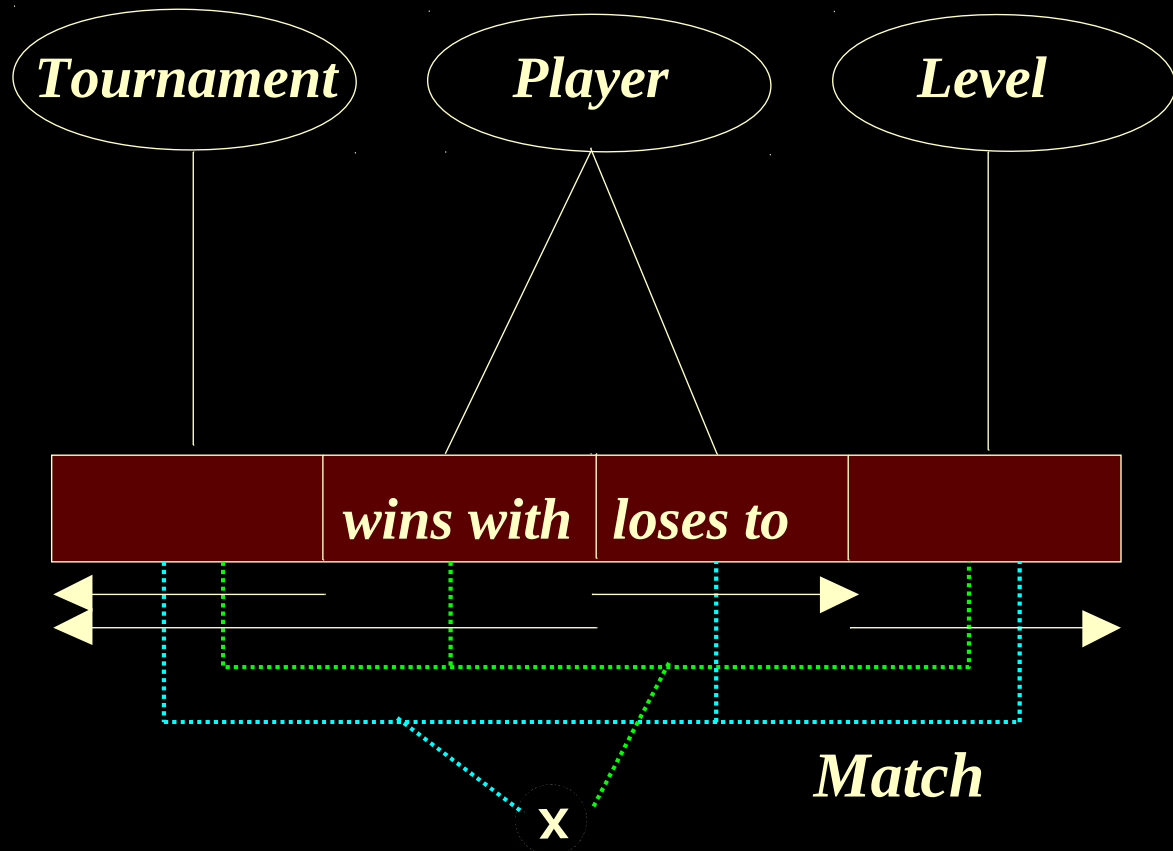
During no stage (Q,S,F) of a tournament one can win a match and lose another match.

Wi	A	Q	Wi	H	Q
Wi	B	Q	Wi	G	Q
Wi	C	Q	Wi	F	Q
Wi	D	Q	Wi	E	Q
...			...		

IT is because above projections of any sample data are disjoint.

# Tennis Tournaments

Tour	Lev	Win	Los
Wi	Q	A	H
Wi	Q	B	G
Wi	Q	C	F
Wi	Q	D	E
Wi	S	E	D
Wi	S	F	C
Wi	F	G	K
Ao	Q	B	D
Ao	S	D	J
. . . . .			



Note, that the above constraints are valid also for data which do not satisfy 'tournament rules'. The compromised data (in green) still satisfy the constraints but they show that it is still possible for the losers in Q to win in S and/or in F. Also, it is not prevented to have other players at the higher stages. The constraints on the diagram do not enforce tournament logistics.

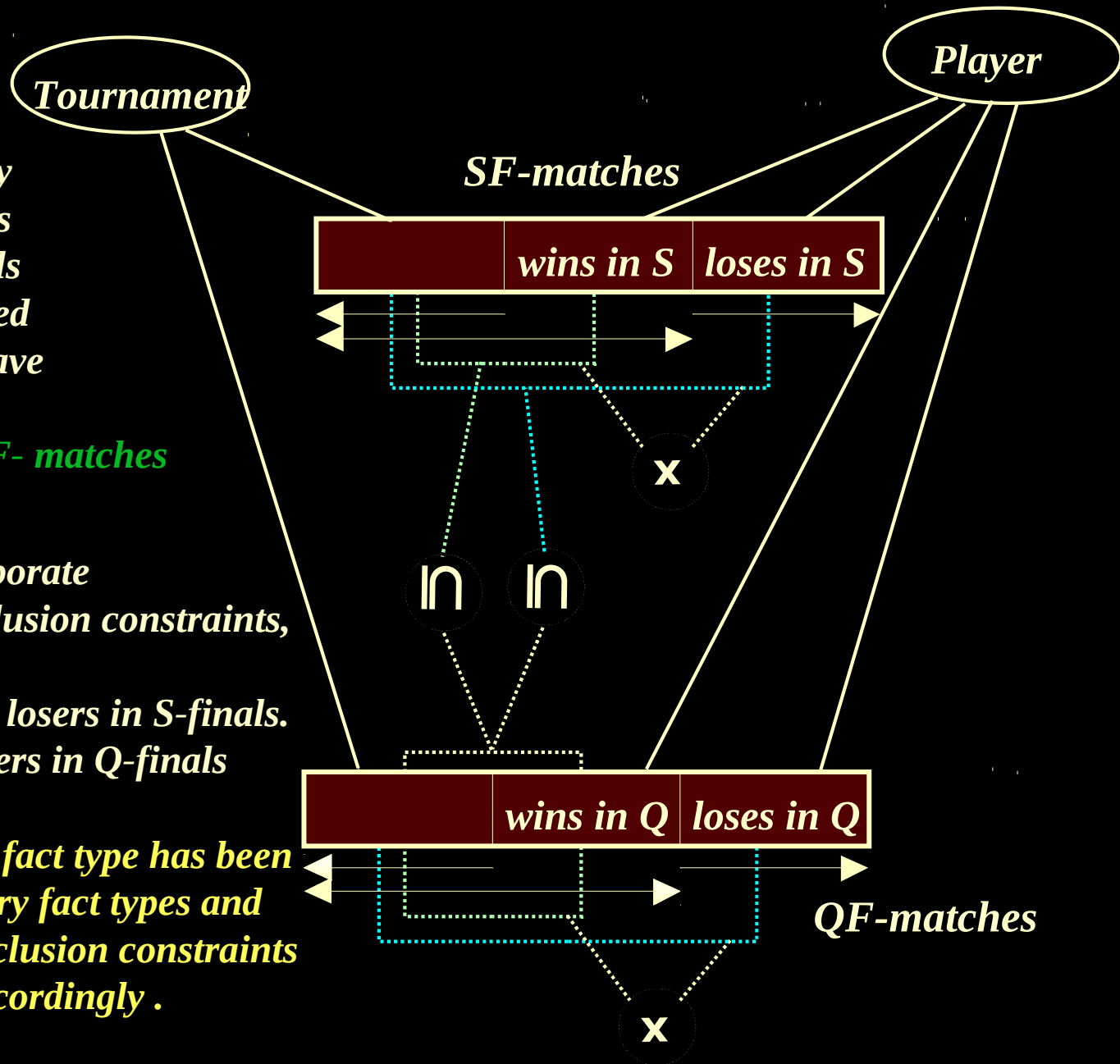
To guarantee, that only winners from Q-finals will advance to S-finals and this will be enforced by our Schema, we have to separate

*QF-matches* and *SF-matches*

Now it is easy to incorporate in the schema two inclusion constraints, one for winners in S-finals and one for losers in S-finals.

All of them are winners in Q-finals

Note that the fortinary fact type has been transformed into ternary fact types and the uniqueness and exclusion constraints have been modified accordingly.





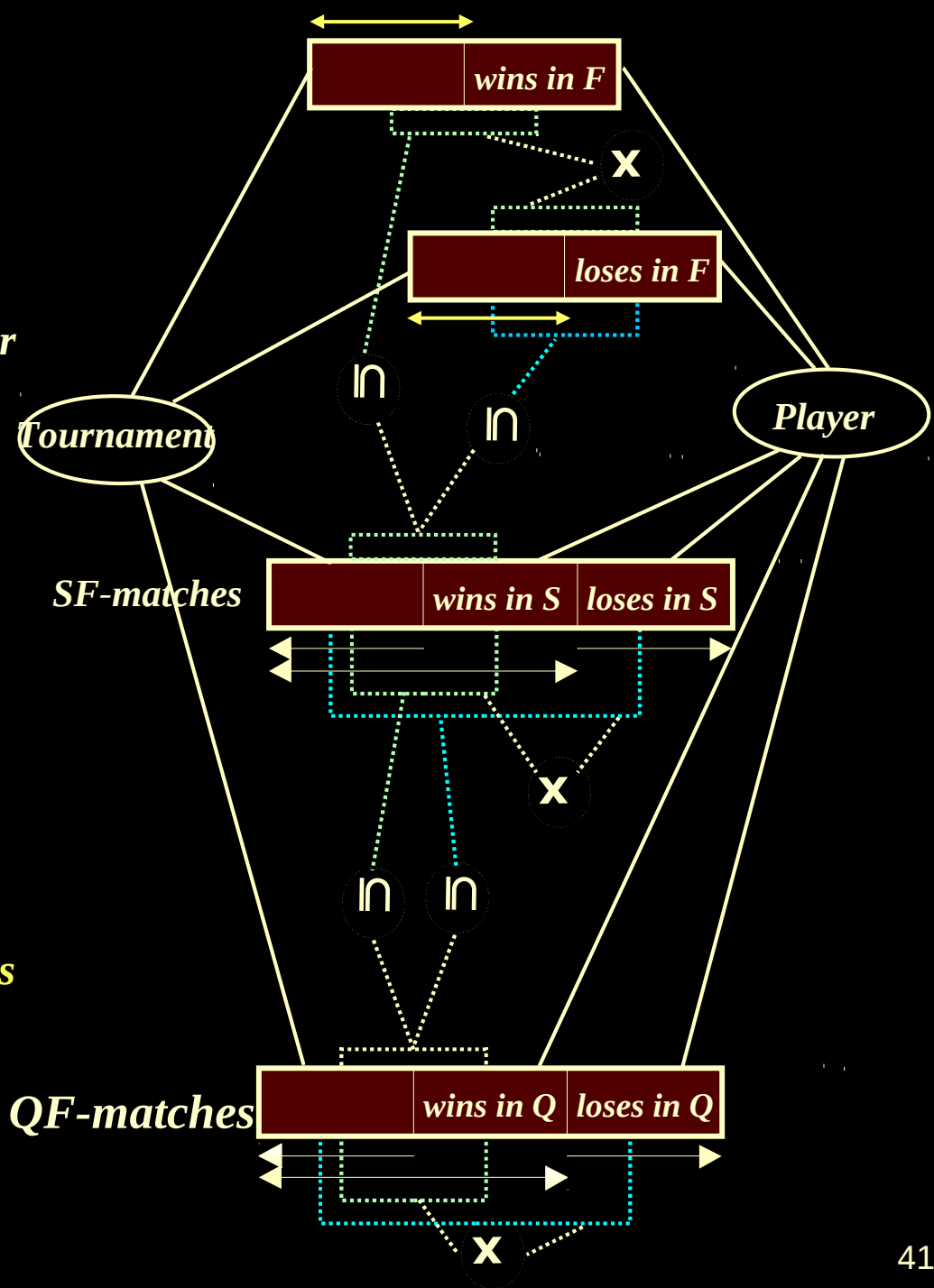
Next we have to ensure that only winners from S-finals advance to Finals.

The relevant Fact Types on the schema differ from the one for Q- or S-finals, since there is only one winner and one loser in Finals of each tournament (\*)

Now, we incorporate an exclusion constraint

...and two inclusion constraints, one for winner in Finals and one for losers in Finals

(\*) Note that one could try to set a ternary fact type for finals, but in this case the uniqueness constraint could be on only one role - for Tournament, and that ternary fact type had to be split



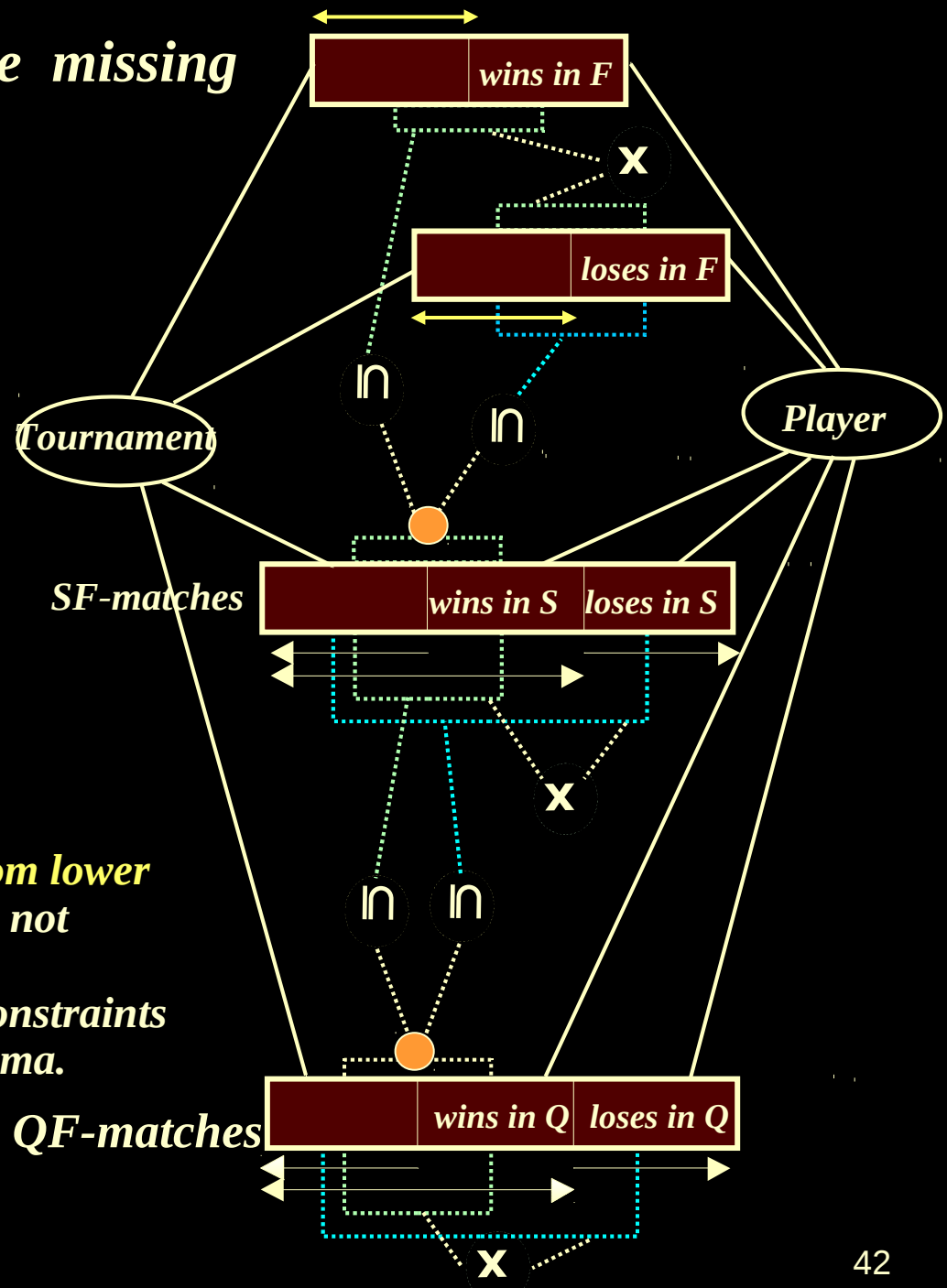
# Still... some constraints are missing

Tour	Lev	Win	Los
Wi	Q	A	H
Wi	Q	B	G
Wi	Q	C	F
Wi	Q	D	E
Wi	Q	X	Z
WI	Q	Y	W
<hr/>			
Wi	S	A	D
Wi	S	B	C
Wi	S	X	Y
<hr/>			
Wi	F	A	B

The requirement: **ONLY** all winners from lower stage have advanced to the next stage is not supported

The above 'corrupted' data satisfy all constraints shown currently on the conceptual schema.

And the medicine is .....

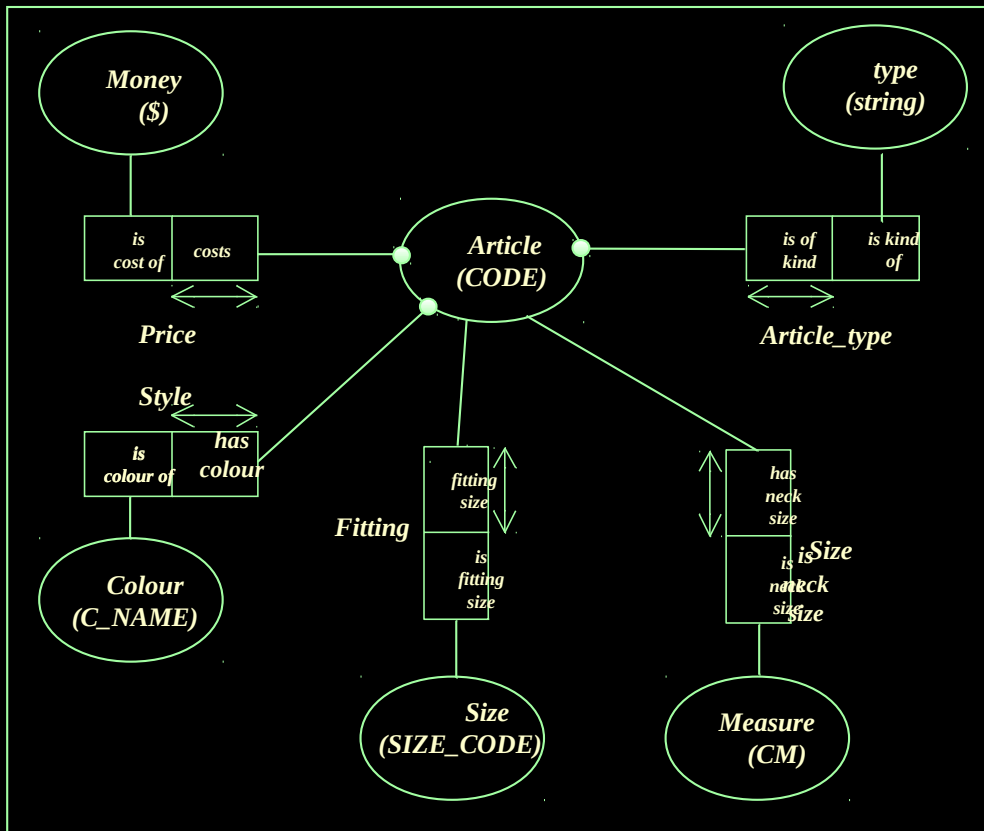


## *Step 6 cont - Subtype construction*

- **The need for subtyping**
- **Method of construction**
  - **Entity-Role matrix**
- **Subtype notation**

Consider the following output report:

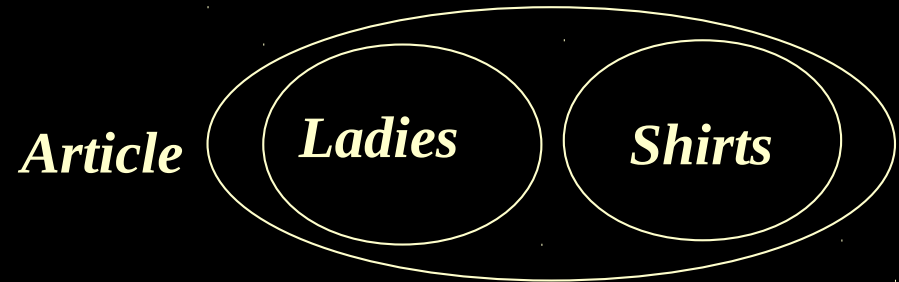
Article	Code	Colour	Price	Size	Neck
Dress	134-6	Red	50.00	14	-
Dress	214-5	Yellow	45.00	12	-
Skirt	712-0	Red	34.95	12	-
Shirt	615-8	White	25.00	-	90
Shirt	547-2	White	50.00	-	85
Shirt	615-9	White	25.00	-	90



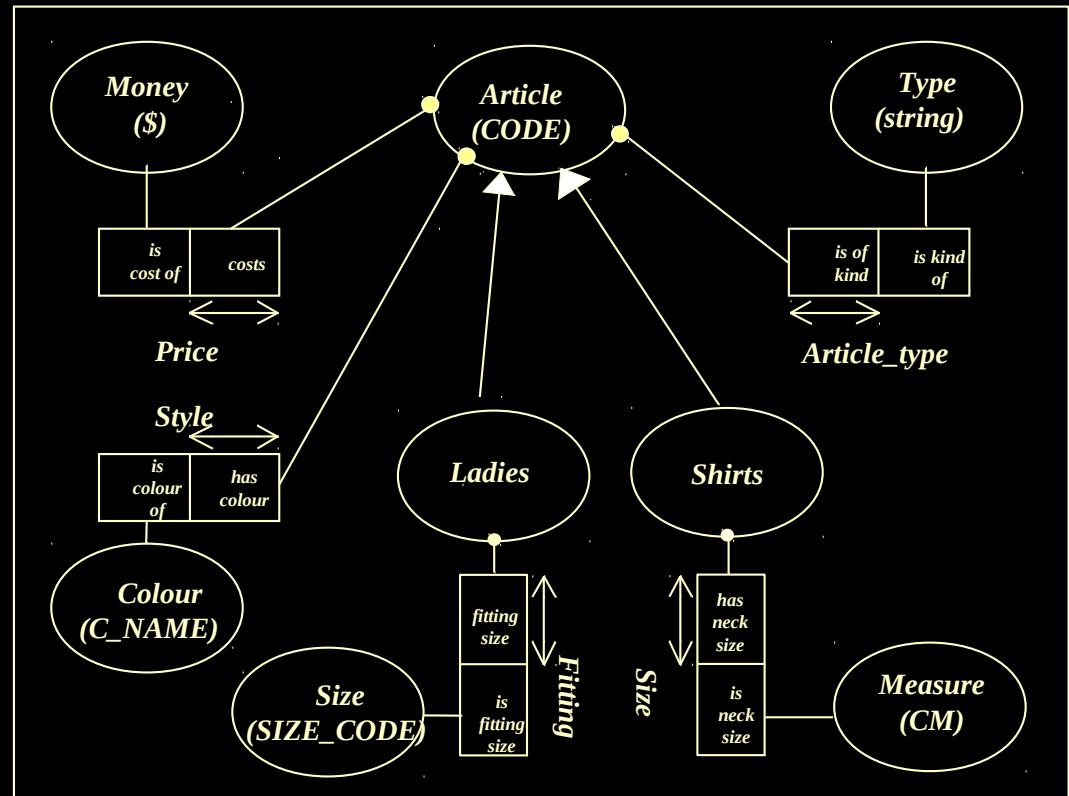
The conceptual schema diagram

From the output report it is evident that **shirts** have a neck size and **skirts and dresses** have a fitting size.

Therefore, although we are concerned with one type of thing, article of clothing, there are variations in the UoD.



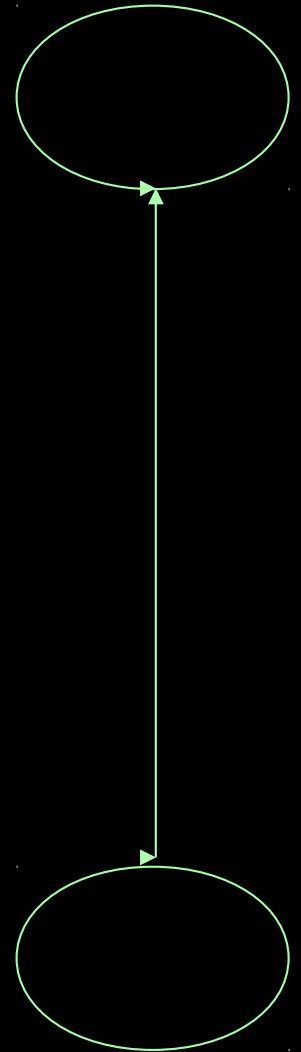
This is shown as follows:



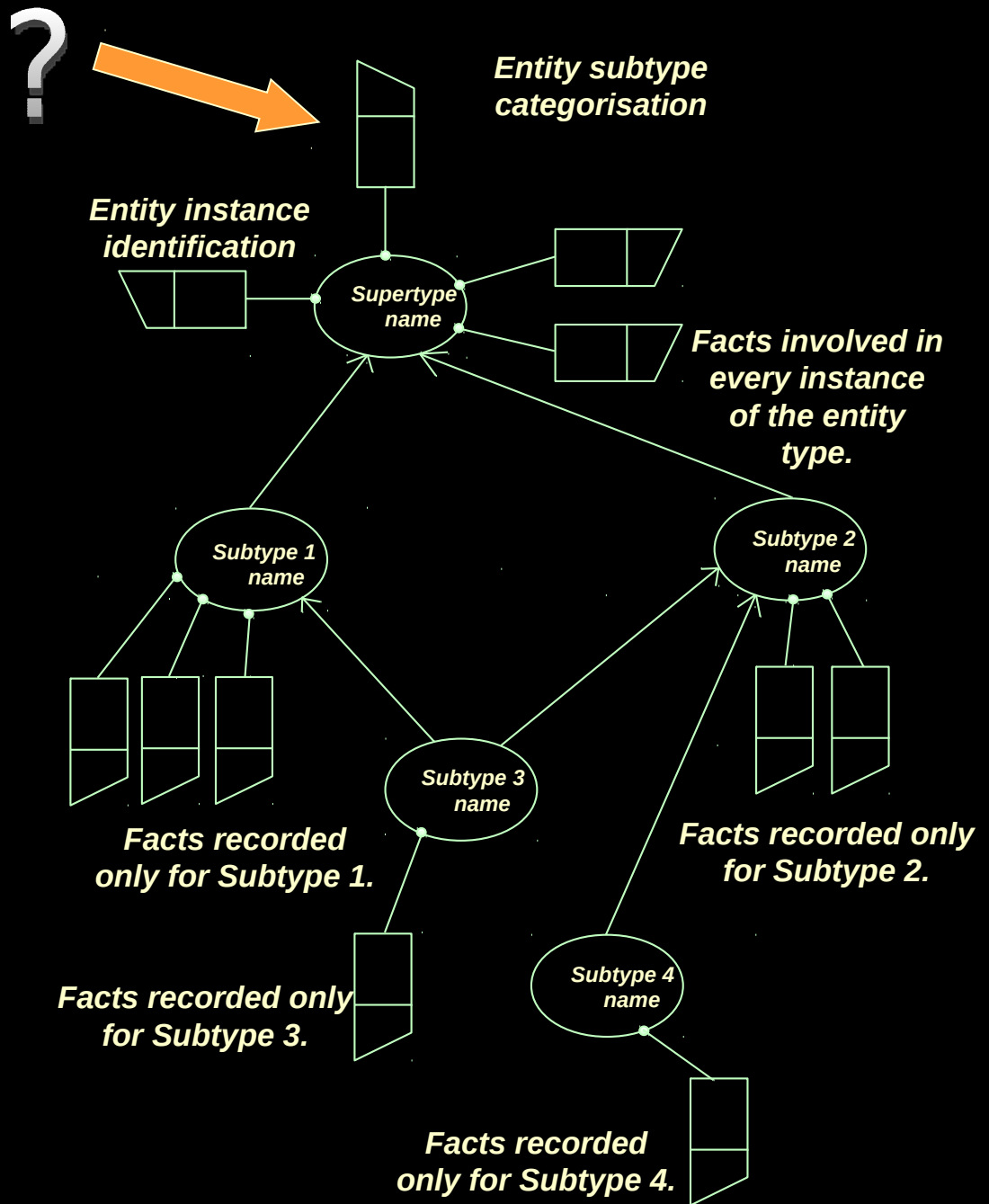
***Supertype: contains the entity type name, and facts giving entity instance identification and subtype categorisation information.***

**The supertype is involved in facts which are to be recorded about every instance of the entity type (total role). The subtype is involved in facts which are to be recorded about every instance of that particular subtype, and no other**

***Subtype: contains the name of the subtype and the facts that relate only to that subtype.***



# General subtype characteristics



## *Entity/Role Matrix*

- 1. Record all *roles* related to an entity type as *columns* in the matrix.**
- 2. Record each *instance* of the entity type as a *row* in the matrix.**
- 3. For each instance, if it participates in a role (i.e. it has a particular property), put 'x' in the corresponding cell; otherwise leave blank.**
- 4. Remove repeating rows.**
- 5. Mark columns (roles) with the same pattern of values 'x'/blank in constructed matrix, and assign to each such pattern an entity sub-type name.**
- 6. In general, an entity type Y is a sub-type of entity type Z iff for each row where Y = 'x', Z = 'x'.**
- 7. Draw the sub-type graph and delete any transitively implied arcs.**



## Example (cont)

<i>Article</i>	<i>Code</i>	<i>Colour</i>	<i>Price</i>	<i>Size</i>	<i>Neck</i>
<i>Dress</i>	<i>134-6</i>	<i>Red</i>	<i>50.00</i>	<i>14</i>	<i>-</i>
<i>Dress</i>	<i>214-5</i>	<i>Yellow</i>	<i>45.00</i>	<i>12</i>	<i>-</i>
<i>Skirt</i>	<i>712-0</i>	<i>Red</i>	<i>34.95</i>	<i>12</i>	<i>-</i>
<i>Shirt</i>	<i>615-8</i>	<i>White</i>	<i>25.00</i>	<i>-</i>	<i>90</i>
<i>Shirt</i>	<i>547-2</i>	<i>White</i>	<i>50.00</i>	<i>-</i>	<i>85</i>
<i>Shirt</i>	<i>615-9</i>	<i>White</i>	<i>25.00</i>	<i>-</i>	<i>90</i>

<i>Article</i>	<i>Code</i>	<i>Colour</i>	<i>Price</i>	<i>Size</i>	<i>Neck</i>
<i>X</i>	<i>X</i>	<i>X</i>	<i>X</i>	<i>X</i>	<i>-</i>
<i>X</i>	<i>X</i>	<i>X</i>	<i>X</i>	<i>X</i>	<i>-</i>
<i>X</i>	<i>X</i>	<i>X</i>	<i>X</i>	<i>X</i>	<i>-</i>
<i>X</i>	<i>X</i>	<i>X</i>	<i>X</i>	<i>-</i>	<i>X</i>
<i>X</i>	<i>X</i>	<i>X</i>	<i>X</i>	<i>-</i>	<i>X</i>
<i>X</i>	<i>X</i>	<i>X</i>	<i>X</i>	<i>-</i>	<i>X</i>

<i>Article</i>	<i>Code</i>	<i>Colour</i>	<i>Price</i>	<i>Size</i>	<i>Neck</i>
<i>X</i>	<i>X</i>	<i>X</i>	<i>X</i>	<i>X</i>	<i>-</i>
<i>X</i>	<i>X</i>	<i>X</i>	<i>X</i>	<i>-</i>	<i>X</i>
<i>A</i>				<i>B</i>	<i>C</i>

In general -

If for every cross in the column representing a set Y there exists a cross in the same rows in a column representing the set Z, then we say that there is a subtype relationship between Y and Z, more precisely: Y is a subtype of Z (notation:  $Y \rightarrow Z$ ).

X	X
	X
X	X
	X
X	X
X	X
Y	Z

Y is a subtype of Z.  
 $Y \rightarrow Z$   
Each cross in column Y has a corresponding cross on the same level in the Z column

X	X
X	
X	X
X	X
	X
	X
X	X
Y	Z

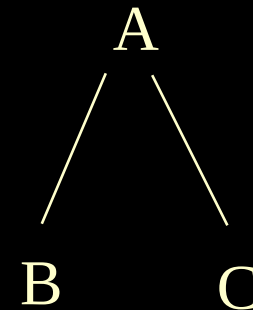
Y is not a subtype of Z.  
Z is not a subtype of Y  
The cross in the second row in column Y has no a corresponding cross on the same level in the column Z.  
Crosses in the fifth and sixth row in the column C have no corresponding crosses in the column Y

## Example (cont)

<i>Article</i>	<i>Code</i>	<i>Colour</i>	<i>Price</i>	<i>Size</i>	<i>Neck</i>
<i>X</i>	<i>X</i>	<i>X</i>	<i>X</i>	<i>X</i>	-
<i>X</i>	<i>X</i>	<i>X</i>	<i>X</i>	-	<i>X</i>
<b>A</b>				<b>B</b>	<b>C</b>

The subtype relationships are:

$B \rightarrow A$  and  $C \rightarrow A$



## Processing of the object role matrix

## Example

Role/ Instance	r1	r2	r3	r4	r5	r6	r7	r8	r9	r10
1	X	X	X	X						
2	X	X	X	X						
3	X	X			X	X	X	X	X	X
4	X	X			X	X			X	X
5	X	X			X	X	X	X	X	
6	X	X								X

*Repeating rows are removed*

*Example*

Role/ Group	r1	r2	r3	r4	r5	r6	r7	r8	r9	r10
(Instance 1&2) 1	X	X	X	X						
2	X	X			X	X	X	X	X	X
3	X	X			X	X			X	X
4	X	X			X	X	X	X	X	
5	X	X								X

*Columns with the same pattern are identified ...*

*Example*

Role/ Group	r1	r2	r3	r4	r5	r6	r7	r8	r9	r10
(Instance 1&2) 1	1	1	1	1						
2	1	1			1	1	1	1	1	1
3	1	1			1	1			1	1
4	1	1			1	1	1	1	1	
5	1	1								1

A B C D E

# Step 5

*Example*

Role/ Group	r1	r2	r3	r4	r5	r6	r9	r7	r8	r10
(Instance 1&2) 1	X	X	X	X						
2	X	X			X	X	X	X	X	X
3	X	X			X	X	X			X
4	X	X			X	X	X	X	X	
5	X	X								X

A B C D E

*... and grouped (for convenience*

r1	r2	r3	r4	r5	r6	r9	r7	r8	r10
X	X	X	X						
X	X			X	X	X	X	X	X
X	X			X	X	X			X
X	X			X	X	X	X	X	
X	X								X
A	B	C	D	E					



***Relationships between column patterns identified  
and consequently relationships between subtypes***

$$B \rightarrow A, C \rightarrow A, D \rightarrow A, E \rightarrow A, D \rightarrow C$$

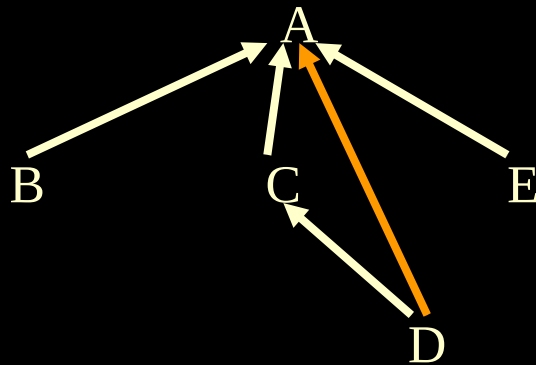
*Every instance (row) with a set of roles B also has a set of roles A.*

*Every instance (row) with a set of roles C also has a set of roles A.*

*Every instance (row) with a set of roles D also has a set of roles C.*

*Every instance (row) with a set of roles D also has a set of roles A.*

*Every instance (row) with a set of roles E also has a set of roles A.*



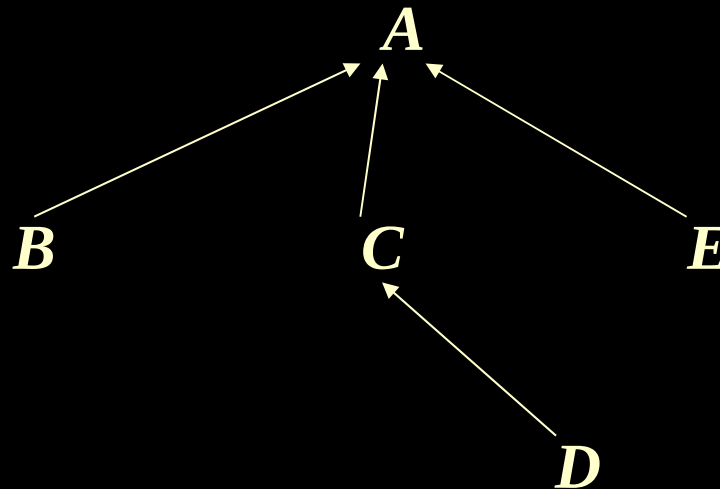
r1	r2	r3	r4	r5	r6	r9	r7	r8	r10
x	x	x	x						
x	x			x	x	x	x	x	x
x	x			x	x	x			x
x	x			x	x	x	x	x	
x	x								x

A      B      C      D      E

***The relationship  $D \rightarrow A$  is redundant as it can be inferred from  
 $D \rightarrow C$  and  $C \rightarrow A$  (transitivity)***

## *Example (cont)*

Draw the sub-type graph and **delete any transitively implied arcs.**



## *Summary*

- **This lecture covered construction of additional constraints:**
  - Complex uniqueness constraints,
  - Subsets constraints and
  - Subtype constraints.
  -
- **The next lecture will continue discussion on sub-typing construction and the final checks.**